

String Physics at Low Energies

→ theoretically viable after '95

New framework for particle physics

alternative to heterotic

Dissociation of string scale M_s from $M_p \Rightarrow$

- brane world description

- strings in accelerators?

→ Protection of hierarchy alternative to susy:

string scale $M_s \sim \text{TeV}$

Outline

- D-brane / type I realization

consistent perturbative framework

for low-scale string models

- gauge hierarchy

- Brane susy breaking

- gauge symmetry breaking

- Standard Model embedding

- NS5-brane / type II realization

alternative LST framework

Realizations of TeV strings

Type I \Rightarrow submm dims

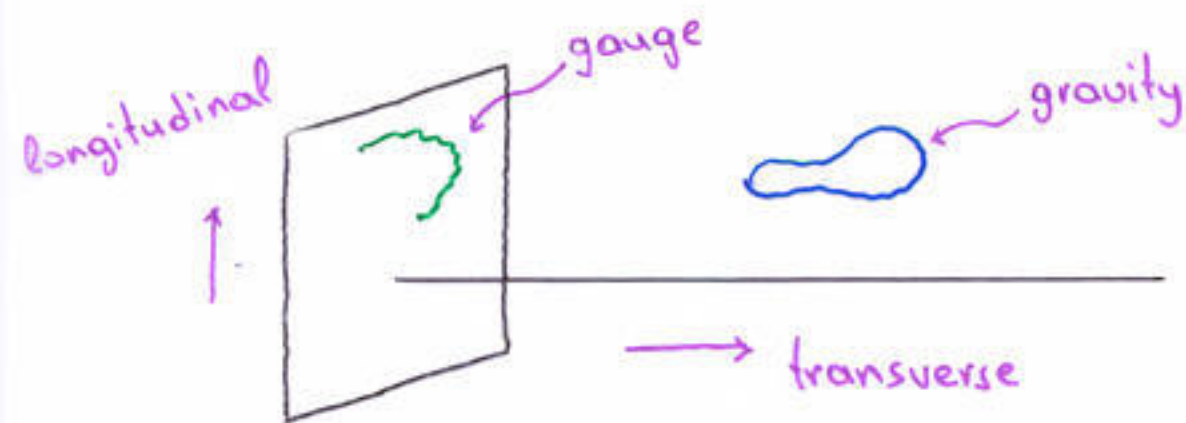
Type II \Rightarrow tiny coupling

strongly coupled Heterotic $SO(32)$ (type I)

$E_8 \times E_8$ (type II)

Type I: closed strings \rightarrow gravity

open strings \rightarrow gauge sector on D-branes



p-brane \Rightarrow p-3 compact dims //

$\underbrace{9-p}_n$ " " \perp

weak coupling \Rightarrow longitud dims \sim string size

transverse dims: no constraint

n \perp dims of radius $r \Rightarrow$

$$M_P^2 = \underbrace{\frac{1}{g^4} M_I^{2+n}}_{M_{P(4+n)}^{2+n}} r^n$$

Planck mass of $4+n$ dims

largeness of $M_P/M_I \Rightarrow$ extra-large r

• string coupling: $\lambda_I = g^2$

• gravity strong at $M_{P(4+n)} \sim M_I \ll M_P$

\uparrow	\uparrow	\uparrow
TeV		10^{19} GeV
10^{-16} cm		10^{-33} cm

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$$M_{P(4+n)}^{2+n}$$

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$M_I \sim 1$ TeV \Rightarrow $n = 2-6$: $r \sim$ mm - fm

Gauge hierarchy

$M_P \gg M_Z \Rightarrow$ why large transverse dims?

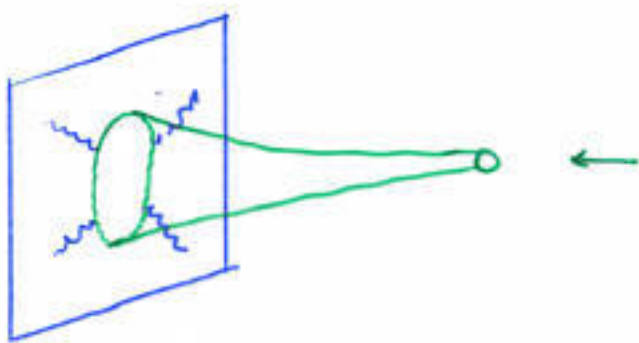
$$r M_I \sim \left(g^2 \frac{M_P}{M_I} \right)^{2/n} \sim \begin{cases} n=2 & 10^{15} \\ n=6 & 10^5 \end{cases} \quad \text{or } \lambda_{II} \approx 10^{-14}$$

Technical aspect: stability in a non susy vacuum

no large corrections to SM couplings as $r M_I \rightarrow \infty$

In general no decoupling if massless bulk fields propagate in less than 2 large transv. dims

I.A. - Bachas '98



IR divergence: emission of massless closed string

UV divergence: open string loop

$d_{\perp} = 1$: linear IR div \Rightarrow quadratic UV $r \sim M_P^2$

Condition: no bulk propagation in one large dim

or local tadpole cancellation \Rightarrow severe constraints

$d_1=2$: log divergences

can be absorbed into a finite number of parameters:

values of bulk massless fields at the brane position

similar to renormalizable field theory

RGE resum \Rightarrow classical 2d eqs in the transverse space

log dependence \Rightarrow higher orders irrelevant

\rightarrow hierarchy could be determined by minim SM eff. potential

\rightarrow No susy TeV strings:

same protection of hierarchy as softly susy at TeV

Do we need susy if $M_{str} \sim \text{TeV}$?

Type I: non susy string models \Rightarrow

$$\Lambda_{\text{bulk}} \sim M_I^{4+n} \Rightarrow \Lambda_{\text{brane}} \sim M_I^{4+n} r^n \sim M_I^2 M_P^2$$

analog of quadratic div. to Λ in softly broken susy

absence of quadratic sensitivity:

- $\Lambda = 0$ (special models)

$$- \Lambda_{\text{brane}} \sim M_I^4 \Rightarrow \Lambda_{\text{bulk}} \sim \frac{M_I^4}{r^n}$$

satisfied if approximate susy in the bulk

e.g. susy is broken primordially only on the brane

explicit realization: Brane susy breaking

I.A. - Dudas - Sagnotti '99

Aldazabal - Uranga '99

No sure in our world (brane)

but it may exist \pm mm away!

to protect the gauge hierarchy against gravit. corrections

Prediction: possible new forces at submm scales

e.g. light scalars: $\frac{(\text{TeV})^4}{M_p} \sim 10^{-4} \text{ eV} = \pm \text{ mm}^{-1}$

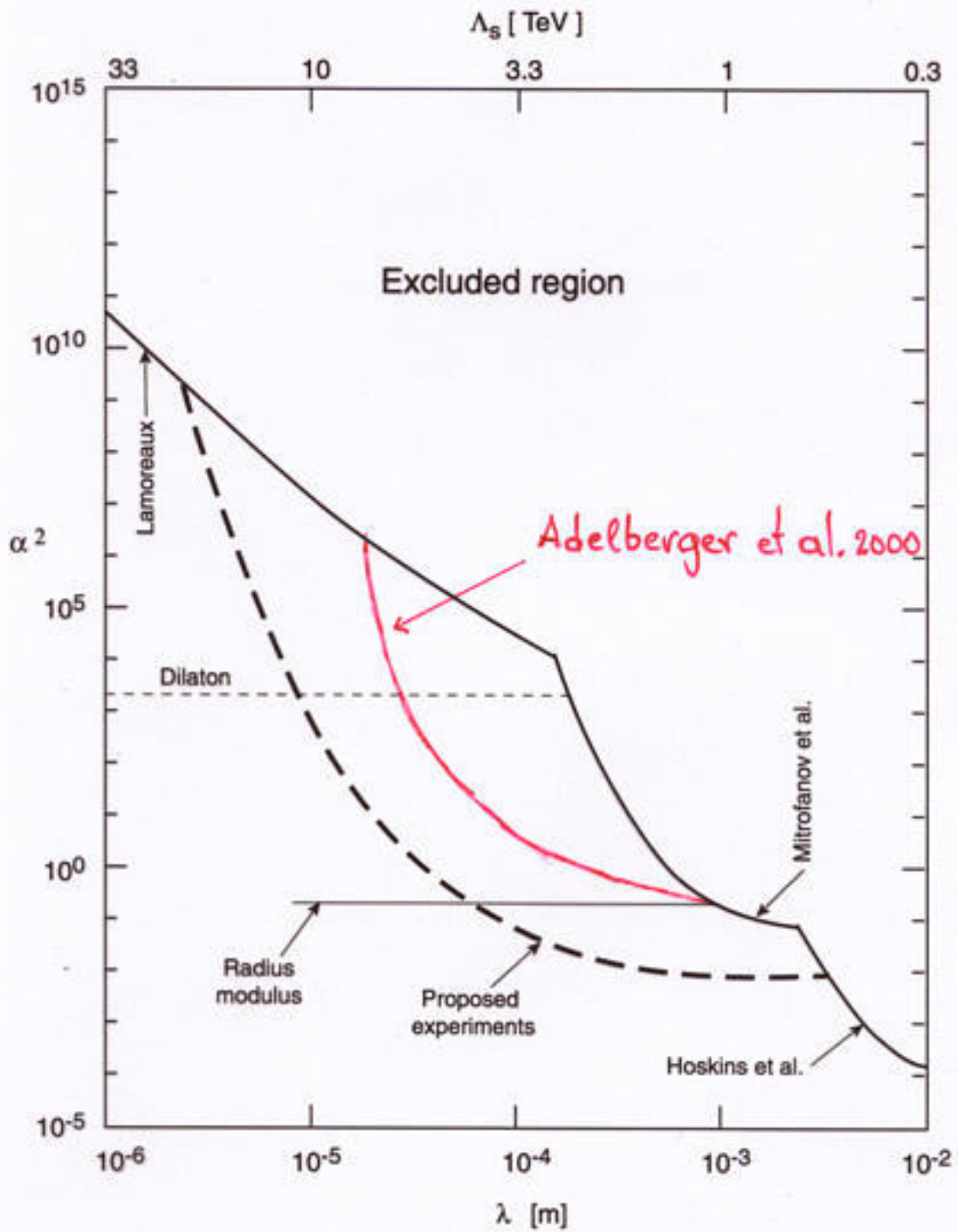
modulus $\equiv \ln r$

coupling to nucleons relative to gravity:

$$\frac{1}{m_N} \frac{\partial m_N}{\partial \ln r} = \frac{\partial \ln \Lambda_{\text{QCD}}}{\partial \ln r} \quad m_N \sim \Lambda_{\text{QCD}} \sim e^{-\frac{1}{b_{\text{QCD}}} \frac{2\pi}{\alpha_{\text{QCD}}}}$$
$$\sim \frac{\partial}{\partial \ln r} \alpha_{\text{QCD}}$$

O(3) in models with log sensitivity in r e.g. $d_1 = 2$

\Rightarrow can be experimentally tested



Brane susy breaking in type I theory

stable non-BPS configurations of

branes - antibranes or branes - anti orientifolds

	RR-charge	tension	(Ns-charge)
D	+	+	
\bar{D}	-	+	
O_{-}	-	-	
\bar{O}_{-}	+	-	
O_{+}	+	+	} as \bar{D}, \bar{O}
\bar{O}_{+}	-	+	

susy : $D\bar{D}$, $D\bar{O}_{+}$, $\bar{D}O_{+}$

absence of tachyons : $D\bar{D}$ of different type

I.A. - Dudas - Sagnotti '99

e.g. $D9 - \bar{D}5$

or in different positions

Aldazabal - Uranga '99

Simplest model 10D $\Pi B / \Omega$ Sugimoto

RR-charge tension

* $\Omega = +1$ \Rightarrow 16 O_9 - -
16 $D9$ + +

open sector: antisymmetrization \Rightarrow $SO(32)$ susy

* $\Omega = -1$ \Rightarrow 16 O_+9 + +
16 $\bar{D}9$ - +

open sector: Ω symmetrizes bosons but
antisymmetrizes fermions

\Rightarrow $Sp(32)$ with fermions in the antisym rep

brane susy breaking $\bar{D}O_+$

Consistent chiral models:

- RR tadpole cancellations \Rightarrow no anomalies
- No tachyons
- susy is broken on $D\bar{5}$ branes
- NS tadpoles \Rightarrow (tree-level) potential

localized on the (non-susy) branes

explicit toy examples:

- T^4/\mathbb{Z}_2 : change Ω projection in the twisted sector
17 tensor multiplets
- $T^6/\mathbb{Z}_2 \times \mathbb{Z}_2$ with discrete torsion
- add $D9 - D\bar{9}$, $D5 - D\bar{5} \Rightarrow$

general class of interesting models

Aldazabal - Ibanez - Quevedo

I.A. - Angelantonj - D'Appollonio - Dudas - Sagnotti

- tree-level potential \Rightarrow fixing the radii
need branes-antibranes of the same type

ex: T^4/\mathbb{Z}_2 $\left\{ \begin{array}{l} \text{untwisted sector: } \Omega = +1 \\ \text{twisted sector: } \Omega = \epsilon = \pm 1 \end{array} \right.$

\swarrow SUSY
 \nwarrow brane SUSY

tadpole conditions:

$$D9 : N_+ \quad \bar{D}9 : N_- \quad D5 : D_+ \quad \bar{D}5 : D_-$$

$$N_+ - N_- = 16$$

$$D_+ - D_- = 16\epsilon$$

$$V_{\text{eff}} = e^{-\phi_6} \left\{ (N_+ + N_- - 16) \sqrt{V_4} + \frac{D_+ + D_- - 16\epsilon}{\sqrt{V_4}} \right\}$$

\uparrow 6D-dilaton

minimization $\Rightarrow V_4 = \frac{D_+ + D_- - 16\epsilon}{N_+ + N_- - 16} = \frac{D_-}{N_-}$

- 1-loop potential \Rightarrow fixing the Wilson lines
 \leftrightarrow branes separation

A toy model

based on T^4/\mathbb{Z}_2 orientifold with brane susy

I.A. - Benakli-Quiroz '99

- 16 non susy anti-D5 branes

all at the origin $\Rightarrow Sp(16) \times Sp(16)$ with

• scalars : $(16, 16)$

• fermions : $(120, 1) + (1, 120) + (16, 16)$

- bulk: gravity + 9-branes

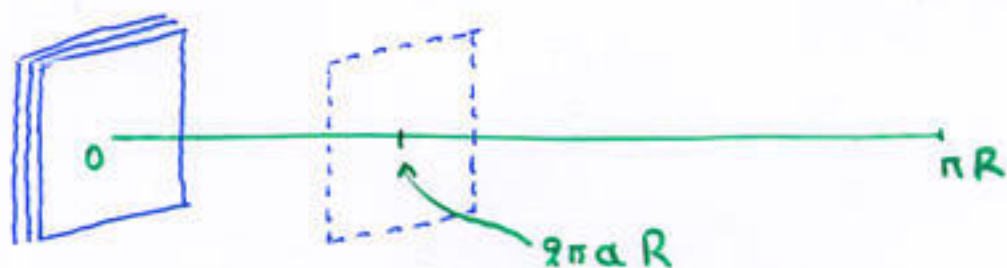
tree-level scalar potential \equiv susy theory

bifundamental hyper-multiplets

$$\Rightarrow V_{\text{tree}} = (\text{D-terms})^2$$

flat directions : $\langle a \rangle \neq 0$

$\bar{D}5$ - brane separation from the origin



1-loop

$$V_{\text{eff}}(a, R) = \frac{R}{32\pi^4} M_s^4 \int_0^\infty \frac{dl}{(2l)^{5/2}} \frac{\theta_2^4}{4\eta^{12}} \left(i l + \frac{1}{2}\right) \sum_n \cos 4\pi n a e^{-2\pi n^2 R^2 l} + a\text{-independent}$$

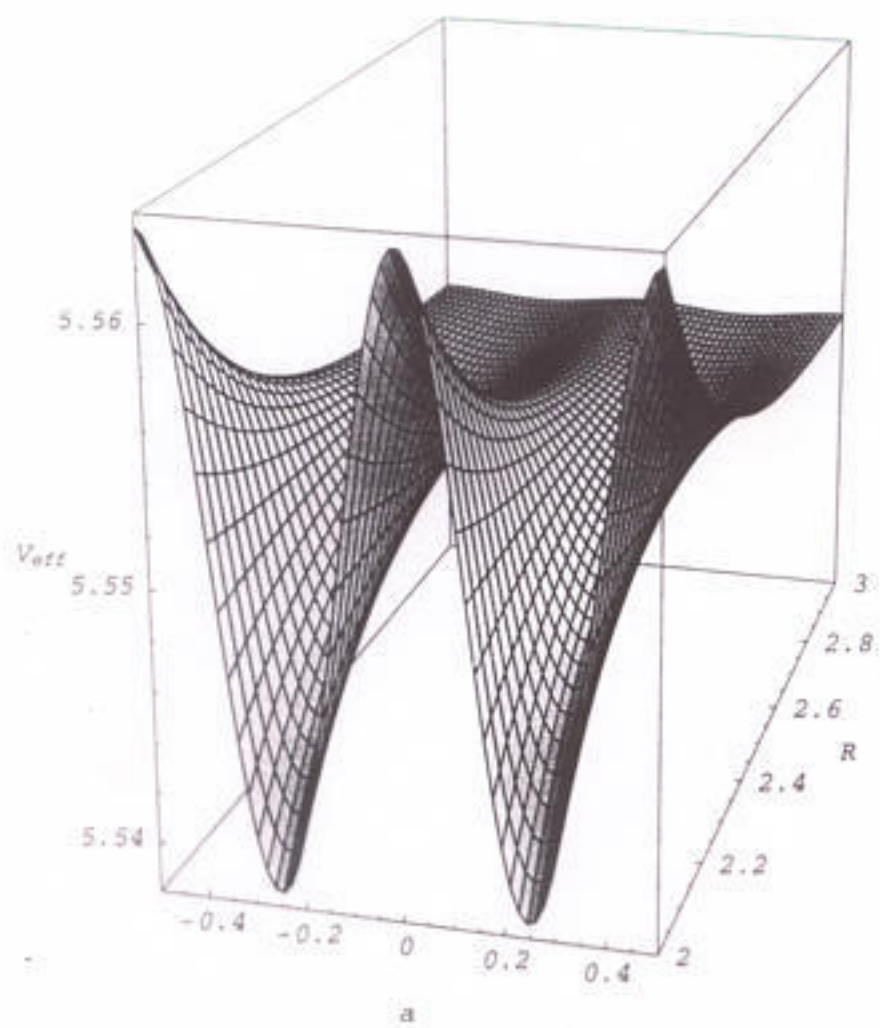
$$V'_{\text{eff}} \sim \sin 4\pi n a = 0 \Rightarrow a = 0, \frac{1}{4}$$

$$V''_{\text{eff}} \Big|_{a=0} < 0 \qquad V''_{\text{eff}} \Big|_{a=\frac{1}{4}} > 0$$

valid for all $a_I = \frac{1}{4} \Rightarrow$ global minimum

all branes in the middle of the comp. interval

$$Sp(16) \times Sp(16) \rightarrow Sp(16)$$



Realistic model: further orbifold projections

→ a is projected away but

computation remains valid for charged components

in the case of susy projections

Framework for Standard Model higgs

→ radiative EW symmetry breaking

$$V = \lambda (h^\dagger h)^2 + \mu^2 (h^\dagger h)$$

• λ given by susy D-terms

• $\mu^2 = -g^2 \epsilon^2 M_s^2 < 0$ at one loop ⇒

- susy prediction for the higgs mass

$$- M_s \sim M_W / \epsilon$$

ϵ : estimated by the previous computation

Expansion around the origin

gauge invariance: $a^2 \rightarrow \text{Tr } \Phi^2$

$$V_{\text{eff}} = V_0 + \frac{1}{2} \mu^2 \text{Tr } \Phi^2 + \mathcal{O}(\Phi^4)$$

$$\mu^2 = -\varepsilon^2(R) g^2 M_s^2$$

$$\varepsilon^2(R) = \frac{R^3}{2\pi^2} \int_0^\infty \frac{dl}{(2l)^{5/2}} \frac{\theta_2^4}{4\eta^{12}} \left(i l + \frac{1}{2} \right) \sum_n n^2 e^{-2\pi n^2 R l}$$

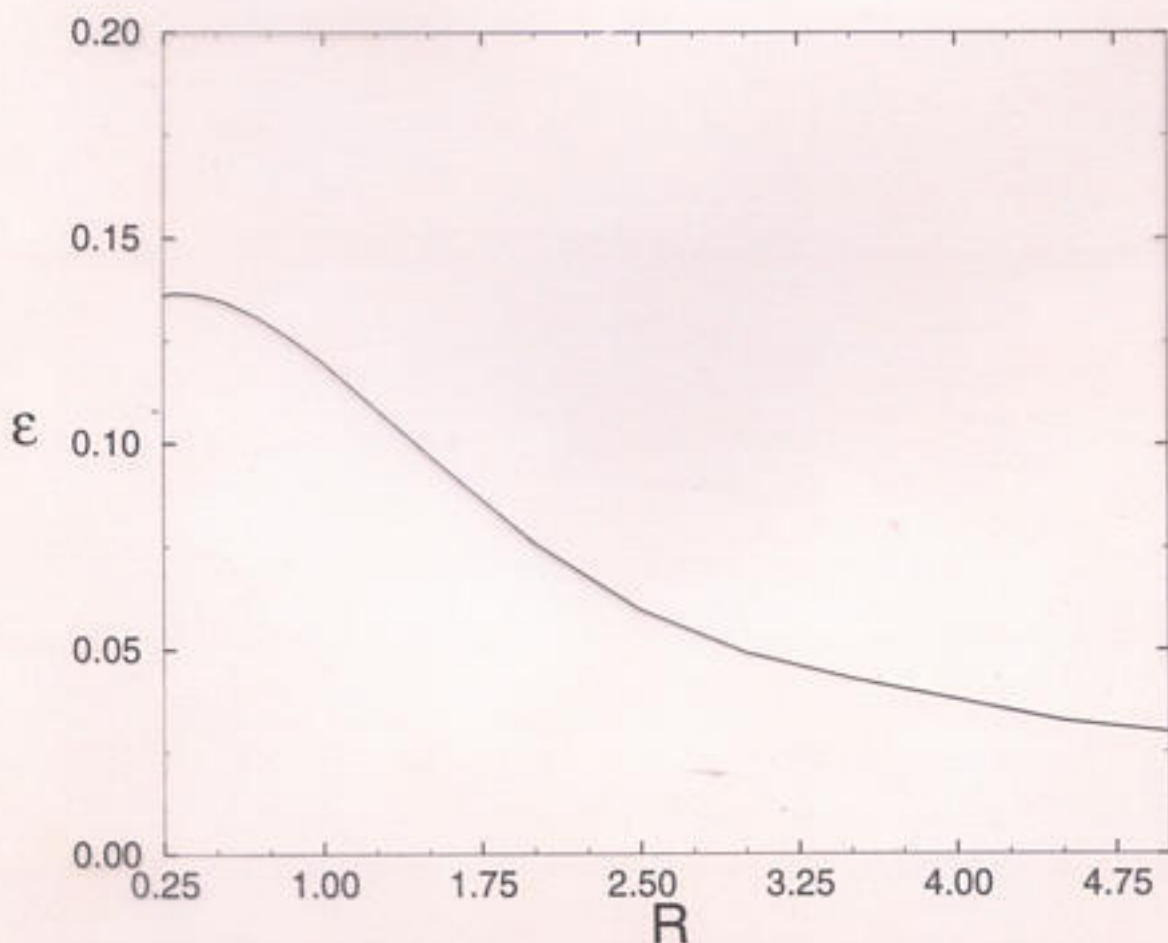
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A D-brane embedding of the Standard Model

I.A. - Kiritsis - Tomaras hep-ph/0004214

N coincident branes $\Rightarrow U(N)$

$$U(1) : \text{coupling} = g_N / \sqrt{2N}$$

with charge of $\frac{N}{2} = 1$

\Rightarrow gauged "baryon" number

\Rightarrow minimal choice : $U(3) \times U(2) \times U(1)$

color branes (g_3) weak branes (g_2) g_1

$$U(1) \text{ brane with } \begin{cases} U(3) \Rightarrow g_1 = g_3 \\ U(2) \Rightarrow g_1 = g_2 \end{cases}$$

fermion generation

$$U(3) \times U(2) \times U(1)$$

$$Q \quad (3, 2; 1, w, 0)_{1/6} \quad w = \pm 1$$

$$u^c \quad (\bar{3}, 1; -1, 0, x)_{-1/3} \quad x = \pm 1 \text{ or } 0$$

$$d^c \quad (\bar{3}, 1; -1, 0, y)_{1/3} \quad y = \pm 1 \text{ or } 0$$

$$L \quad (1, 2; 0, 1, z)_{-1/2} \quad z = \pm 1 \text{ or } 0$$

$$e^c \quad (1, 1; 0, 0, 1)_1$$

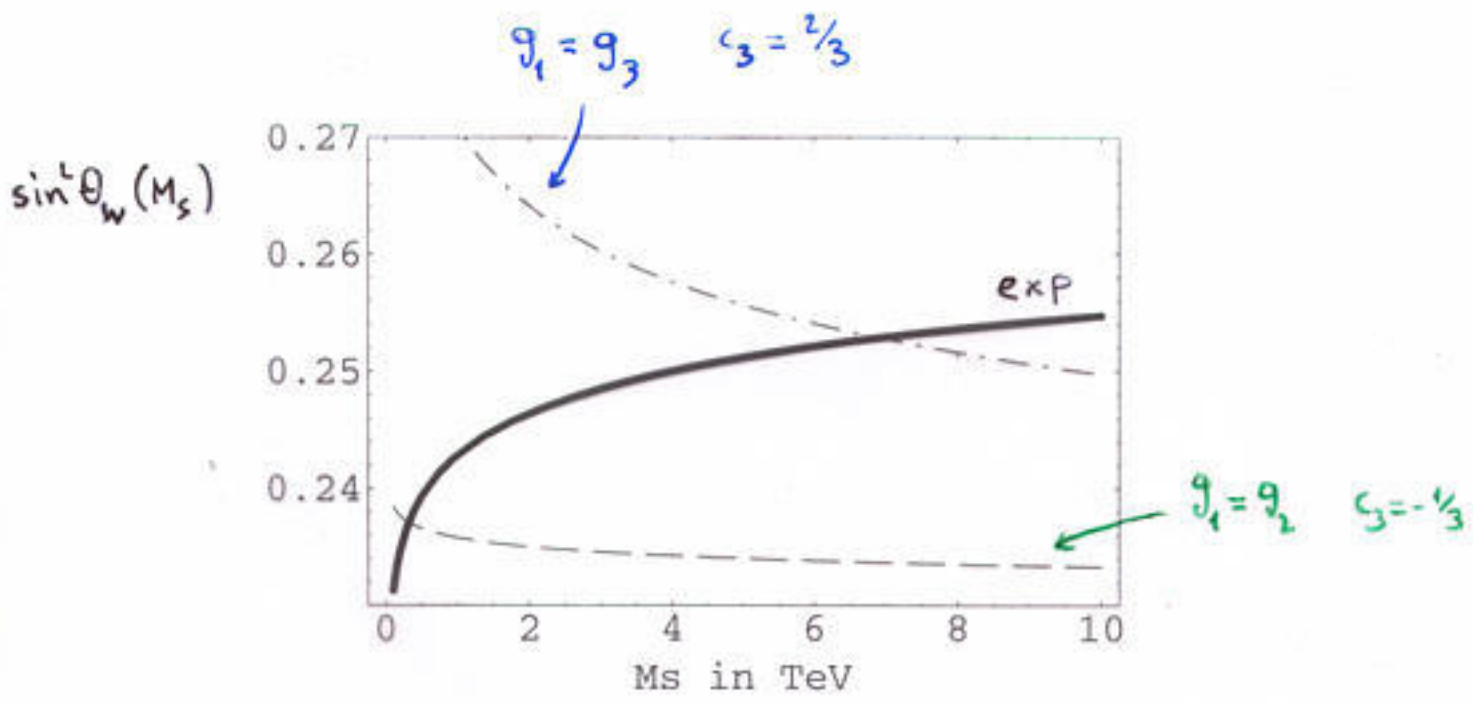
hypercharge $Y = c_1 Q_1 + c_2 Q_2 + c_3 Q_3 \Rightarrow 4$ possibilities

$$c_3 = -1/3 \quad c_2 = \pm 1/2 \quad x = -1 \quad y = 0 \quad w = \pm 1 \quad z = -1/0$$

$$c_3 = 2/3 \quad c_2 = \pm 1/2 \quad x = 0 \quad y = 1 \quad w = \mp 1 \quad z = -1/0$$

$$\sin^2 \theta_w = \frac{1}{2 + 2 \frac{g_2^2}{g_1^2} + 6 c_3^2 \frac{g_2^2}{g_3^2}}$$

$$g_1 = g_2 = g_3 \Rightarrow \sin^2 \theta_w = \begin{cases} \frac{3}{14} & c_3 = -\frac{1}{3} \\ \frac{3}{20} & c_3 = \frac{2}{3} \end{cases}$$



correct prediction for $\sin^2 \theta_w$ for $M_s \sim$ few TeV

$U(1)$ with color branes

$$U(3) \times U(2) \times U(1)$$

$$\text{hypercharge } Y = \frac{2}{3} Q_3 - \frac{1}{2} Q_2 + Q_1$$

$$Q \quad (3, 2; 1, 1, 0)$$

$$u^c \quad (\bar{3}, 1; -1, 0, 0)$$

$$d^c \quad (\bar{3}, 1; -1, 0, 1)$$

$$L \quad (1, 2; 0, 1, 0)$$

$$e^c \quad (1, 1; 0, 0, 1)$$

$$\text{Higgs: } H \quad (1, 2; 0, 1, 1) \quad H' \quad (1, 2; 0, -1, 0)$$

$$\Rightarrow H^c Q u^c \quad H^+ L e^c \quad H^+ Q d^c$$

- masses to all quarks + leptons \Rightarrow 2 Higgs doublets
- the remaining two $U(1)$'s : anomalous

Green-Schwarz anomaly cancellation:

shifting of 2 axions \Rightarrow $U(1)$'s become massive

\Rightarrow global (perturbative) symmetries:

- baryon number \Rightarrow proton stability
- PQ-type symmetry \Rightarrow electroweak axion



can be explicitly broken by moving slightly

away from the orbifold point $e^{-m/\lambda}$

- R-neutrinos : open strings in the bulk $H^c L \nu_R$

Arkani Hamed - Dimopoulos - Dvali - March Russell

Dienes - Dudas - Gherghetta '98

- mixed $U(1)_A$ - non abelian anomalies

$$k_i = \text{Tr} Q_A T_i^2 \Rightarrow$$

$$(\partial a + g_A A)^2 + a \sum_i k_i \text{Tr} F_i \wedge F_i$$

$$A \rightarrow A + \partial \Lambda$$

$$a \rightarrow a - g_A \Lambda$$

Dine - Seiberg - Witten

- mixed $U(1)_A$ - abelian anomalies

$$\bullet k_Y = \text{Tr} Q_A Y^2 \Rightarrow \text{same as non abelian}$$

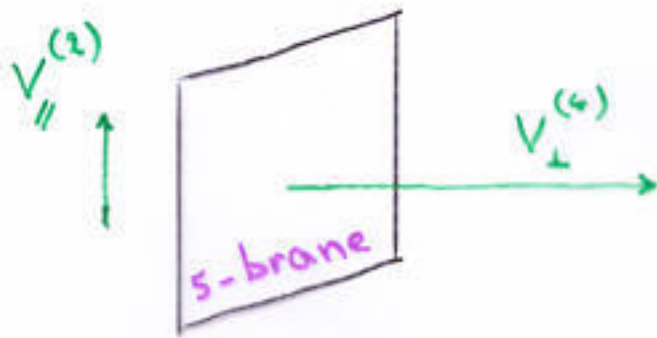
$$\bullet \xi = \text{Tr} Y Q_A^2 \Rightarrow \text{Chern-Simons terms:}$$

$$\xi \left(-A_Y \wedge \omega_A + a F_Y \wedge F_A \right)$$

Type II strings

I.A. - Poline '99

Non abelian symmetries: non-perturbative on a 5-brane
localized at singularities of the internal manifold \nwarrow_{NS}



$$M_P^2 = \frac{1}{\lambda_{II}^2} \frac{1}{g^2} M_S^{2+4} V_{\perp}^{(4)}$$

New possibility: largeness of $M_P \Rightarrow$ tiny string coupling

$$\text{all radii} \sim M_S^{-1}, \quad \lambda_{II} \approx 10^{-14}$$

- No strong gravity at TeV

- signal: 2 longitudinal (TeV) dims $V_{\parallel}^{(2)}$

with gauge interactions

similar in Heterotic with small instantons

Benakli-03

$\lambda_{II} \rightarrow 0 \Rightarrow$ Little String Theory at low energies

I.A. - Dimopoulos - Giveon to appear

- Gauge interactions on NS5-branes

$$\text{NS5 on } T^2 \Rightarrow g^2 \sim \begin{cases} 1/R_1 R_2 & \text{type IB} \\ R_2/R_1 & \text{type IA} \end{cases}$$

IB: 0-branes

endpoints of D-strings on NS5's

$$T_0 = T_{D1} L \equiv M_w \quad L: \text{separation}$$

IA: "charged" strings

endlines of D2-branes on NS5's

$$T_1 = T_{D2} L = M_w / R_1 \quad \leftarrow \text{T-duality from IB}$$

- Neutral closed little strings

trapped in the vicinity of 5-branes

double scaling limit: $\lambda_{\text{II}} \rightarrow 0$, $L \rightarrow 0$

$$g_{\text{LST}} = \frac{\lambda_{\text{II}}}{LM_s} = \begin{cases} M_s/M_W & \text{II B} \\ M_s^2/T_1 & \text{II A} \end{cases}$$

$$\text{II B: } R_{4,r}^{-1} < M_s \quad \text{but} \quad g_{\text{LST}} > 1$$

$$\text{II A: } g_{\text{LST}} < 1 \Rightarrow M_s < \sqrt{T_1} < R_{4,r}^{-1}$$

\Rightarrow little strings: first signal of new physics!

- stability of hierarchy : automatic

- fixing $\lambda_{\text{II}} \sim 0 \Rightarrow$ need $\ln \lambda_{\text{II}}$ corrections
to the effective potential

In principle YES if anomalous $U(1)_A$

in a D-brane "hidden" sector

$$m_A \sim g_A M_s \quad g_A^2 \sim \lambda_{\text{II}} \Rightarrow \ln m_A^2 \sim \ln \lambda_{\text{II}}$$

- dilaton coupling to matter : ultraweak

$$\sim \lambda_{\text{II}} / M_p \sim \mathcal{O}(1/M_p^2)$$

\Rightarrow no exp constraint on its mass

- $\Lambda < \mathcal{O}(M_s^4)$

$\Lambda < \Lambda_{\text{exp}} \Rightarrow \Lambda = 0$ up to 2 loops

$$\Lambda_{\text{3-loops}} \sim \lambda_{\text{II}}^4 M_s^4 \sim \frac{M_s^8}{M_p^4}$$