

STRONGLY COUPLED
GRAVITY AND
CONFORMAL INVARIANCE

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REVIEWS IN CONFERENCE
PROCEEDINGS:

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STRONG COUPLING LIMITS

→ DUAL THEORY

COMPACTIFIED STRING THEORY:

$$\lambda = e^{\langle \phi \rangle} \rightarrow \infty$$

→ BOUNDARY OF MODULI SPACE, LOSING SCALARS

STRONG GRAVITY

LIMIT $L_{\text{PLANCK}} \rightarrow \infty$

KEEPING ALL SCALARS

i.e. CONSIDER ENERGIES

$$E \gg 1 / L_{\text{PLANCK}}$$

DUAL THEORY ?

D=5 N=4 SYM

$g_{YM}^2 \rightarrow \omega :-$

(ROZALI)

D=6 (2,0) CFT

FOR FREE (ABELIAN) THEORY

$A_N \rightarrow B_{MN}^+$

D=5 N=8 SUPERGRAVITY

$L_{\text{PLANCK}} \rightarrow \omega :$

D=6 (4,0) CFT

FOR FREE THEORY

$g_{\mu\nu} \rightarrow C_{MNPQ}^+$

NON-RENORMALIZABLE LOW
ENERGY EFFECTIVE THEORIES
OF CONSISTENT THEORIES

N=4 SUPER YANG-MILLS

D=4: $SL(2; \mathbb{Z})$

S-DUALITY GOVERNS STRONG
COUPLING BEHAVIOUR

D=5

$g_{YM}^2 = L$ LENGTH SCALE

NON-RENORMALIZABLE,
EFFECTIVE THY $E \ll 1/g_{YM}^2$

REGARD AS SECTOR OF
CONSISTENT THEORY

e.g. D=5 HETEROTIC STRING

D4 - BRANE

(MODEL FOR GRAVITY)

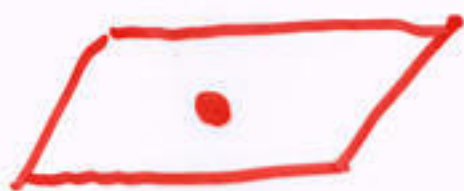
$D = 5$ $g_{YM}^2 \rightarrow \infty$ ($E \gg 1/g_{YM}^2$)

- EXPECT TO KEEP(?)

16 SUSY'S, $SO(5)$ R-SYMMETRY,

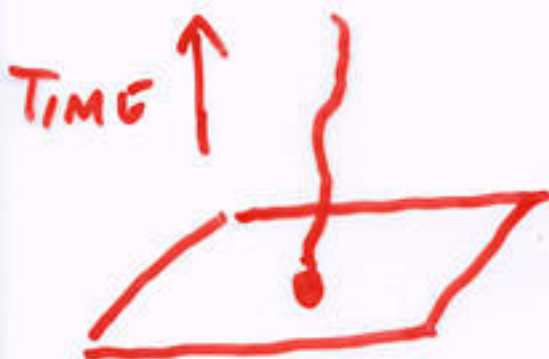
ALL $5 \times \dim(G)$ SCALARS

- BUT EXTRA LIGHT STATES



INSTANTON IN \mathbb{R}^4

$$F = *F$$



0-BRANE IN

4+1 DIMS

$$\text{MASS} \propto n/g_{YM}^2 \rightarrow 0$$

KALUZA KLEIN TOWER FOR
6TH DIMENSION, RADIUS = g_{YM}^2

STRONG COUPLING LIMIT:—

$D=6$ (2,0) CFT (ROZALI)

- UNIQUE $D=6$ THEORY
WITH 16 SUSYS, $SO(5)_R$
 $5 = \dim(G)$ SCALARS
- SUPERCONFORMAL
- $g_{YM}^2 = R$ COMPACTIFICATION
MODULUS
ON S^1_R , GET $D=5$ SYM
FOR $E \ll \tau \ll 1/R$

D4-BRANE

→ M5-BRANE
WRAPPED ON S^1_R

D=5 HETEROTIC STRING

→ IIB ON $K3 \times S^1_R$

D=5 SYM SECTOR

→ D=6 (2,0) CFT
SECTOR

WHICH CAN BE CONSIST.
DECOUPLED

ABELIAN SYM

D=4: $SL(2)$ SYMMETRY
OF FIELD EQUATIONS

D=5

ABELIAN (2,0) D=6:

$(B_{MN}, \lambda, \phi^i)$

$dB \simeq * (dB), \quad i=1, \dots, 5$

REDUCE ON S^1_R :

D=5 SYM

$$S \sim \int \frac{1}{R} F^2 + \dots$$

EXPLICIT CHECKS

NON-ABELIAN SYM

D=4 $SL(2)$ NOT

SYMMETRY OF FIELD THEORY

D=5 NO LOCAL COVARIANT

D=6 (2,0) INTERACTIONS

THAT CAN GIVE D=5 SYM

GOOD EVIDENCE FOR

DUALITIES \rightsquigarrow

LOCAL CONVENTIONAL

FIELD THEORY NOT

COMPLETE DESCRIPTION?

NEW KIND OF THEORY
IN $D = 6$ WITH "M-INTERACTIONS"

\downarrow T^2

$D = 4$ THEORY WITH "M-INTS"

- MANIFEST $SL(2; \mathbb{Z})$
- REDUCES TO SYM

OTHER CORNERS OF

M-THEORY WITH

M-INTERACTIONS?

D=5 N=8 SUGRA

SECTOR OF M-THEORY ON T^6

E_6 RIGID \times $USp(8)$ LOCAL

$\hookrightarrow E_6(\mathbb{Z})$

$g_{\mu\nu}$

A_μ 27 ABELIAN

ϕ 42 IN $E_6/USp(8)$

$$L \sim \frac{1}{l_p^3} R + \frac{1}{l_p} F^2 + \dots$$

5-D PLANCK LENGTH l_p

STRONG COUPLING $l_p \rightarrow \infty$

- SEEK DUAL THEORY WITH
32 SUSYS, 42 SCALARS,
 $USp(8)$ SYMM

$N=8 \rightarrow N=4$ MULTIPLETS

EACH $N=4$ VECTOR MULT

$\rightarrow D=6 (2,0)$ MULT B_{MN}^+ , ...

$USp(8) \Rightarrow$ ALL 27 $A_\mu \rightarrow B_{MN}^+$

$\Rightarrow D=6$ THEORY WITH
27 SELF-DUAL B_{MN}^+ , 42 ϕ

SUPERCONFORMAL

BUT UNIQUE $D=6$ "N=8"
SUGRA FAILS ALL THESE
POINTS

(4, 0) SUPERMULT IN D=6

- 42 SCALARS, 27 B_{MN}^+
- $USp(8)$ R-SYMMETRY
- SUPERCONFORMAL
 $OSp^*(8/8) \supset SO(6,2) \times USp(8)$
32 + 32 SUSY'S!
- REDUCTION ON S'_R
OF FREE (4,0) THEORY
→ LINEARISED D=5 SUGRA
 $L_p = \text{RADIUS}$

IMMEDIATE CANDIDATE
FOR STRONG COUPLING
LIMIT

NO GRAVITON, BUT
FIELD IN $(5, 1)$ OF $SU(5) \times SU(2)$

→ GAUGE FIELD

C_{MNPQ}

SYMMS OF
RIEMANN TENSOR

FIELD STRENGTH

$$G_{MNPQRS} = G_{[MNP][QRS]} \\ \sim \partial\partial C$$

SELF - DUAL

$$G = *G = G*$$

$$G_{MNPQRS} = \frac{1}{6} \epsilon_{MNP TUV} G^{TUV}_{QRS}$$

FREE $(4, 0)$ THEORY IN FLAT
 $D=6$ SPACETIME BACKGROUND
EXISTS.

INTERACTING FORM?

AS FOR $(2, 0)$, NO LOCAL
COVARIANT INTS.

M-INTERACTIONS?

THERE SHD BE NO ROLE FOR
 $D=6$ METRIC IN SUCH
A THEORY

D=5 LINEARISED GRAVITY:

$$\delta h_{\mu\nu} = \partial_{(\mu} \xi_{\nu)}$$

LIFTS TO D=6 GAUGE INV

$$\delta C_{MNPQ} = \partial_{[M} \chi_{N]PQ} + \partial_{[P} \chi_{Q]MN}$$

$$\chi_{MPQ} = -\chi_{MQP}, \quad \chi_{[MPQ]} = 0$$

LINEARISED D=6 THEORY
ALSO HAS SYMMETRY UNDER
DIFFEOS OF BACKGROUND
SPACETIME.

NOT CLEAR (!) IF INTERACTING
THEORY SHOULD BE A
DIFFEO THEORY ON A D=6
SPACETIME MANIFOLD

ANY $D=6$ DIFFEO THEORY
REDUCED ON T^2 GIVES
 $D=4$ THEORY WITH $SL(2; \mathbb{Z})$

ABELIAN (2,0): $D=4$ $F_{\mu\nu}$

$$\mathcal{F} \sim \begin{pmatrix} F \\ *F \end{pmatrix} \quad \mathcal{F} \rightarrow S \mathcal{F}$$

LINEAR (4,0): $D=4$ $R_{\mu\nu\rho\sigma}$

$$\mathcal{R} \sim \begin{pmatrix} R & *R \\ R^* & *R^* \end{pmatrix}$$

$$\mathcal{R} \rightarrow S \mathcal{R} S^t$$

S-DUALITY
SYMMETRIES OF FREE $D=4$:

ABELIAN SYM,
LINEARISED SUPERGA

NOT SYMMETRIES OF
INTERACTING $D=4$ FIELD
THEORIES - $N=4$ SYM, $N=8$
SUGRA

IF M -INTERACTING
DIFFEO $(2,0)$ OR $(4,0)$ EXIST,
REDUCTION ON T^2 GIVES
 M -INTERACTING $D=4$
THEORIES WITH MANIFEST
S-DUALITY

CONVENTIONAL SYM OR
SUGRA WOULD BE LIMITS?

GRAVITATIONAL S-DUALITY?

BPS STATES

27 0-BRANES &

27 STRINGS IN $D=5$ (A_{26})

→ 27 SELF-DUAL

STRINGS IN $D=6$ (B_{mn}^+)

$D=6$ MOMENTUM MODES

~ $D=5$ "INSTANTONIC"

0-BRANES.

(SINGULAR) SOLUTIONS
OF $D=5$ SUGRA

IMPORTANT CHECK: THESE
SHD CORRESPOND TO
STATES IN BPS SPECTRUM

• STRONG COUPLING LIMIT
OF $D=5$ LINEARISED SUGRA

→ $D=6$ FREE $(4,0)$

• CAN $l_p \rightarrow \infty$ LIMIT OF
INTERACTING $D=5$ THEORY

GIVE NON-TRIVIAL

M -INTERACTING THEORY?

• IF SO, MANY IMPLICATIONS
FOR PLANCK SCALE GRAVITY
& M -THEORY

$$g_{\mu\nu} \rightarrow C_{MNPQ}^+$$

GEOMETRY → ?

• VAST SYMMETRY

- LIMITS OF M-THEORY ONT⁶
IN WHICH O-BRANES
BECOME MASSLESS WOULD
LIFT TO TENSIONLESS
STRING LIMITS IN $D=6$
- POSSIBILITY OF A $(4,0)$
SCFT WITH "TENSIONLESS
STRINGS" GIVING
QUANTUM SUPERGRAVITY
ON REDUCTION
- CLOSELY RELATED TO
 $(2,0)$ THEORY, AND
UNDERSTANDING THIS WOULD
BE AN IMPORTANT STEP
- M-INTS, NOT FIELD THY?