

## STRINGS-2 012 Gong Show

Alessandra Gnecchi Padua University, Italy



# DUALITY INVARIANCE FOR BLACK HOLES IN N=2 GAUGED SUPERGRAVITY

with G. Dall'Agata, JHEP 1103 (2011) 037 + work in progress...

## N=2, U(1)-GAUGED SUPERGRAVITY

Scalar potential mimics a cosmological constant

Solutions now depend on BH charges and parameters of the

gauging

 $p^{\Lambda} = rac{1}{4\pi} \int_{\mathcal{C}^2} \mathbf{F}^{\Lambda} , \qquad q_{\Lambda} = rac{1}{4\pi} \int_{\mathcal{C}^2} \mathbf{G}_{\Lambda} ,$ 

Beyond asymptotically flat geometries, AdS4 Cvetic et al., Duff & Liu, Sabra 1998-2003

Cacciatori & Klemm, 2009

Existence of extremal BPS solutions with horizon geometry  $AdS_2 \times S^2$  and finite horizon radius, first order equations

related works: Hristov, Toldo & Vandoren, 2011

## STATIC BLACK HOLES METRIC ANSATZ

$$ds^{2} = -e^{2U(r)}dt^{2} + e^{-2U(r)}(dr^{2} + e^{2\psi(r)}d\Omega^{2})$$

$$AdS_2 \times S^2$$
 AdS<sub>4</sub>

$$\partial_i \mathcal{W} = 0$$

$$D_i \mathcal{L} = 0$$

## Double attractor condition

- More constraints on the fields
- Less solutions less easily found

## DUALITY COVARIANT BPS FLOW

Fully symplectic vector of gauge couplings  $\mathcal{G} = (g^{\Lambda}, g_{\Lambda})$ 

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$$\mathcal{L} = \langle \mathcal{G} \,, \mathcal{V} 
angle$$

$$\mathcal{L} = \langle \mathcal{G}, \mathcal{V} \rangle \qquad \qquad \mathcal{Z} \equiv \langle Q, \mathcal{V} \rangle$$

BPS first order flow driven by the superpotential

$$\mathcal{W} = e^U |\mathcal{Z} - ie^{2(\psi - U)}\mathcal{L}|$$

BPS constraints ~ Charge quantization condition

$$\langle \mathcal{G}, Q \rangle + 1 = 0$$

cfr. Romans, '92

1/4 - BPS condition

$$\gamma^{0} \epsilon_{A} = i e^{i\alpha} \varepsilon_{AB} \epsilon^{B}$$
$$\gamma^{1} \epsilon_{A} = e^{i\alpha} \delta_{AB} \epsilon^{B}$$

## ATTRACTOR EQUATIONS

$$Q + e^{2A} \Omega \mathcal{M} \mathcal{G} = -2 \operatorname{Im}(\overline{\mathcal{Z}} \mathcal{V}) + 2 e^{2A} \operatorname{Re}(\overline{\mathcal{L}} \mathcal{V})$$

$$e^{2A} = -i\frac{\mathcal{Z}}{\mathcal{L}} = R_S^2$$

Interesting relation for the black hole entropy



$$e^{-2A} = 2\left(|D_i\mathcal{L}|^2 - |\mathcal{L}|^2\right)$$

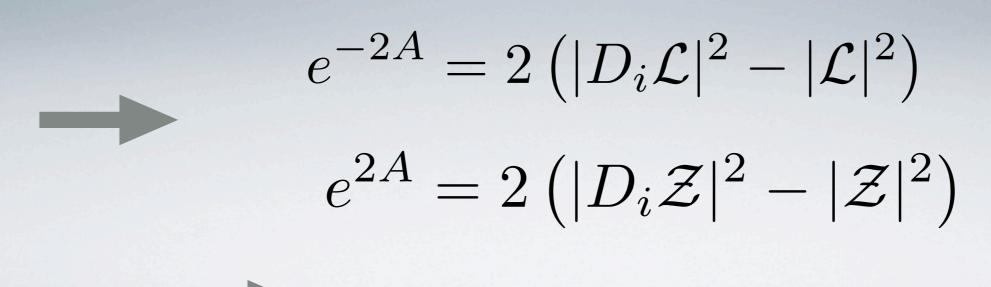
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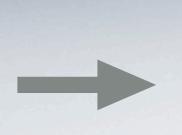


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Any geometric interpretation?

#### MORE SOLUTIONS

**Extensions to multicenter BHS** 

Analogous derivation of the base space to Breitenlohner-Maison-Gibbons '88 analysis

First order equations for rotating solutions

introduce 
$$\mathbf{G} = \mathcal{G}e^i dx^i$$
  $\mathbf{L} \equiv \langle \mathbf{G}, \mathcal{V} \rangle$ 

$$\frac{1}{2}e^{V-U} \star_0 d\omega + \langle \mathcal{I}, d\mathcal{I} \rangle - e^{-2U} \operatorname{Re}(e^{-i\alpha - V} \mathbf{L}) = 0$$

$$\mathcal{P}_I^x = \xi_I e^x \delta_x^I \quad \text{SU(2)} \sim \text{SO(3)}$$

