



# STRINGS-2 012 Gong Show

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## DUALITY INVARIANCE FOR BLACK HOLES IN $N=2$ GAUGED SUPERGRAVITY

*with G. Dall'Agata, JHEP 1103 (2011) 037  
+ work in progress...*

# N=2, U(1)-GAUGED SUPERGRAVITY

Scalar potential mimics a cosmological constant

Solutions now depend on BH charges and parameters of the gauging

$$p^\Lambda = \frac{1}{4\pi} \int_{S^2} F^\Lambda, \quad q_\Lambda = \frac{1}{4\pi} \int_{S^2} G_\Lambda, \quad g_\Lambda$$



Beyond asymptotically flat geometries, AdS<sub>4</sub>

**Cvetič et al., Duff & Liu, Sabra 1998–2003**

**Cacciatori & Klemm, 2009**

Existence of extremal BPS solutions with horizon geometry

$AdS_2 \times S^2$  and finite horizon radius, first order equations

related works: *Hristov, Toldo & Vandoren, 2011*



# STATIC BLACK HOLES

## METRIC ANSATZ

$$ds^2 = -e^{2U(r)} dt^2 + e^{-2U(r)} (dr^2 + e^{2\psi(r)} d\Omega^2)$$

$$AdS_2 \times S^2 \longleftrightarrow AdS_4$$

$$\partial_i \mathcal{W} = 0$$

$$D_i \mathcal{L} = 0$$

Double attractor condition

- 📌 More constraints on the fields
- 📌 Less solutions less easily found

# DUALITY COVARIANT BPS FLOW

Fully symplectic vector of gauge couplings  $\mathcal{G} = (g^\Lambda, g_\Lambda)$

$$\mathcal{L} = \langle \mathcal{G}, \mathcal{V} \rangle \quad \mathcal{Z} \equiv \langle Q, \mathcal{V} \rangle$$

BPS first order flow driven by the superpotential

$$\mathcal{W} = e^U |\mathcal{Z} - i e^{2(\psi - U)} \mathcal{L}|$$

BPS constraints ~ Charge quantization condition

$$\langle \mathcal{G}, Q \rangle + 1 = 0$$

cfr. Romans, '92

1/4 - BPS condition

$$\begin{aligned} \gamma^0 \epsilon_A &= i e^{i\alpha} \varepsilon_{AB} \epsilon^B \\ \gamma^1 \epsilon_A &= e^{i\alpha} \delta_{AB} \epsilon^B \end{aligned}$$



# ATTRACTOR EQUATIONS

$$Q + e^{2A} \Omega \mathcal{M} \mathcal{G} = -2\text{Im}(\bar{\mathcal{Z}} \mathcal{V}) + 2 e^{2A} \text{Re}(\bar{\mathcal{L}} \mathcal{V})$$

$$e^{2A} = -i \frac{\mathcal{Z}}{\mathcal{L}} = R_S^2$$

Interesting relation for the black hole entropy



$$e^{-2A} = 2 \left( |D_i \mathcal{L}|^2 - |\mathcal{L}|^2 \right)$$

$$e^{2A} = 2 \left( |D_i \mathcal{Z}|^2 - |\mathcal{Z}|^2 \right)$$

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Any geometric interpretation?

## MORE SOLUTIONS


### Extensions to multicenter BHS

Analogous derivation of the base space to Breitenlohner–Maison–Gibbons '88 analysis

### First order equations for rotating solutions

introduce  $\mathbf{G} = \mathcal{G}e^i dx^i$      $\mathbf{L} \equiv \langle \mathbf{G}, \mathcal{V} \rangle$

$$\frac{1}{2}e^{V-U} \star_0 d\omega + \langle \mathcal{I}, d\mathcal{I} \rangle - e^{-2U} \text{Re}(e^{-i\alpha-V} \mathbf{L}) = 0$$

  $\mathcal{P}_I^x = \xi_I e^x \delta_x^I$      $\text{SU}(2) \sim \text{SO}(3)$





Thank You