

Entanglement, gravity and tensor networks

Review talk

Juan Maldacena

Strings 2016

Beijing

Motivation

- How does quantum gravity work ?

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- How are its degrees of freedom encoded ?

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→ Follow the qubit !

Outline

- Ancient concepts \rightarrow quantum entropy

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- Quantum entropy in QFT.

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- Quantum entropy in semiclassical gravity

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- Wormholes

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- Wormholes
- Tensor networks

Quantum entropy

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Quantum entropy

- State $\rightarrow \rho$
- Quantum entropy: $S = -\text{Tr}[\rho \log \rho]$
- Modular Hamiltonian.

$$K = -\log \rho , \quad \rho = e^{-K}$$

Makes the density matrix look “thermal”

- Relative entropy

$$S(\rho|\sigma) = \text{Tr}[\rho \log \rho] - \text{Tr}[\rho \log \sigma]$$

- Relative entropy

$$\begin{aligned} S(\rho|\sigma) &= \text{Tr}[\rho \log \rho] - \text{Tr}[\rho \log \sigma] \\ &= -\Delta S + \Delta K \sim \Delta F \end{aligned}$$

Looks like the
“free energy”

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Measure of the distinguishability of states

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Measure of the distinguishability of states

- Positivity $S(\rho|\sigma) \geq 0$

- Relative entropy

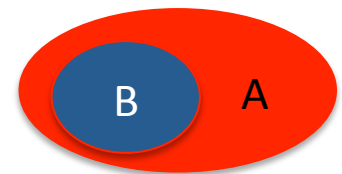
$$S(\rho|\sigma) = \text{Tr}[\rho \log \rho] - \text{Tr}[\rho \log \sigma]$$

$$= -\Delta S + \Delta K \sim \Delta F$$

Looks like the
“free energy”

Measure of the distinguishability of states

- Positivity $S(\rho|\sigma) \geq 0$
- Monotonicity



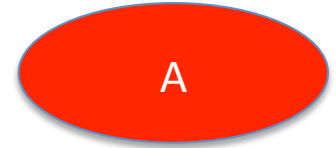
$$B \subset A \longrightarrow S(\rho_B|\sigma_B) \leq S(\rho_A|\sigma_A)$$

Looking at less, we can distinguish less

In quantum field theory

Entropy in QFT

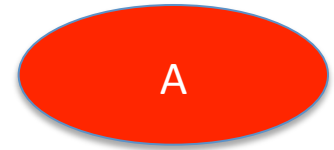
- Quantum entropy of subregions.



Entropy in QFT

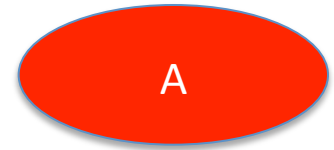
- Quantum entropy of subregions.
- Divergent

$$S(A) = \frac{\text{Area}}{\epsilon^2} + \dots + \text{Finite}$$



Entropy in QFT

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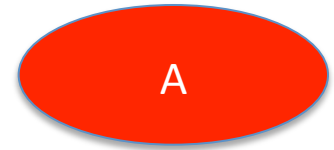
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- Interesting: Finite results.

Entropy in QFT

- Quantum entropy of subregions.



- Divergent

$$S(A) = \frac{\text{Area}}{\epsilon^2} + \dots + \text{Finite}$$

- Interesting: Finite results.
- Recall the QFT is a “target” for what we should approximately get in the bulk.

Half space in relativistic QFT

Bisognano Wichmann, Unruh

- Half space \rightarrow Thermal in Rindler space
- Consequence of the Lorentz symmetry

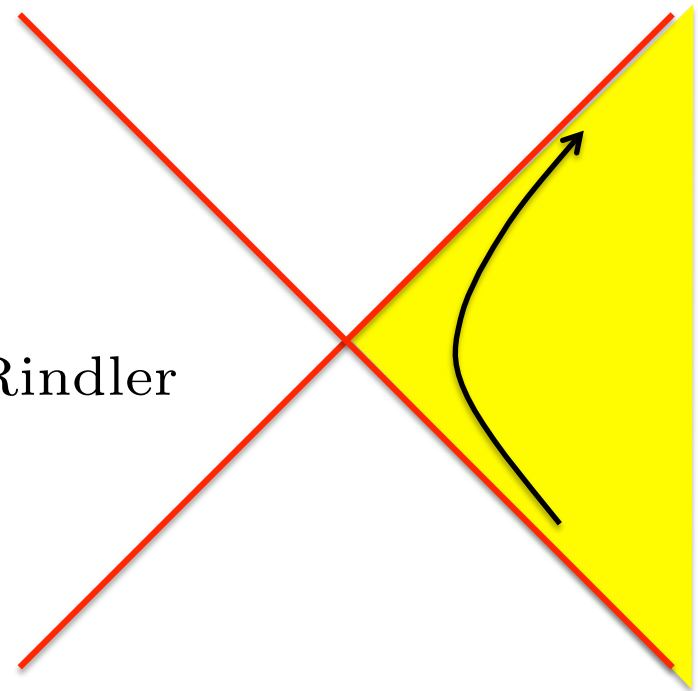
$$\rho = e^{-2\pi B}$$

$$B = \int_0^\infty d^{D-2}y dx x T_{00} = E_{\text{Rindler}}$$



Local

Energy for accelerating observer



Entanglement → useful results in QFT

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- Bekenstein-Casini bound :

Sorkin
Marolf, Minic Ross
Casini

$$S(\rho|\rho_v) \geq 0 \longrightarrow \Delta S \leq 2\pi \langle \Delta B \rangle = 2\pi \langle \Delta E_R \rangle$$

Relative entropy is UV finite

Entanglement → useful results in QFT

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- c and f theorems (in 1+1 and 2+1 dimensions)

Casini Huerta

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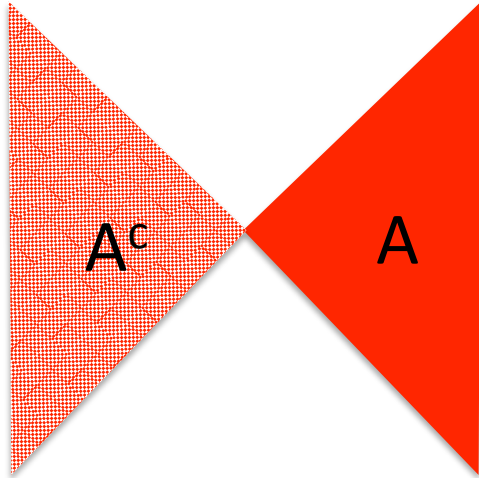
Casini Huerta

- Integrated null energy condition (integrated along a null line)

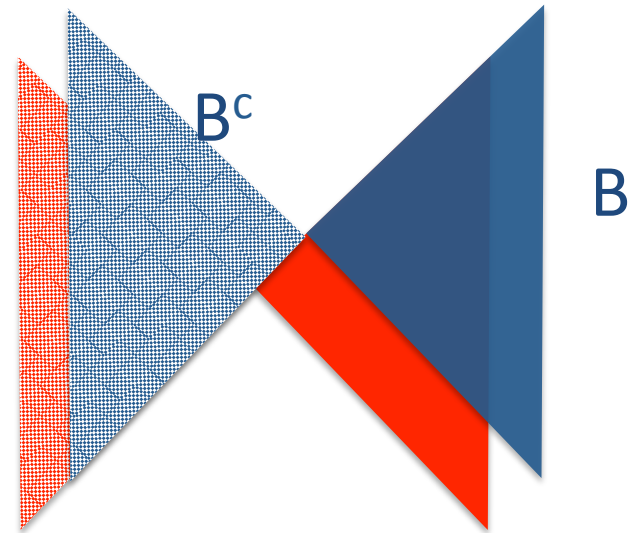
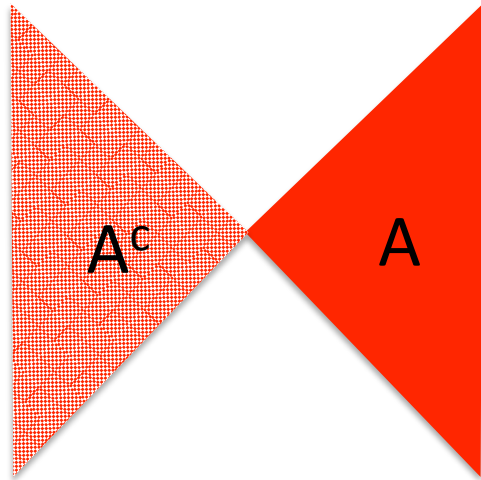
$$\langle \int dx^- T_{--}(x^-, x^+, \vec{y}) \rangle \geq 0$$

Faulkner, Leigh, Parrikar, Wang

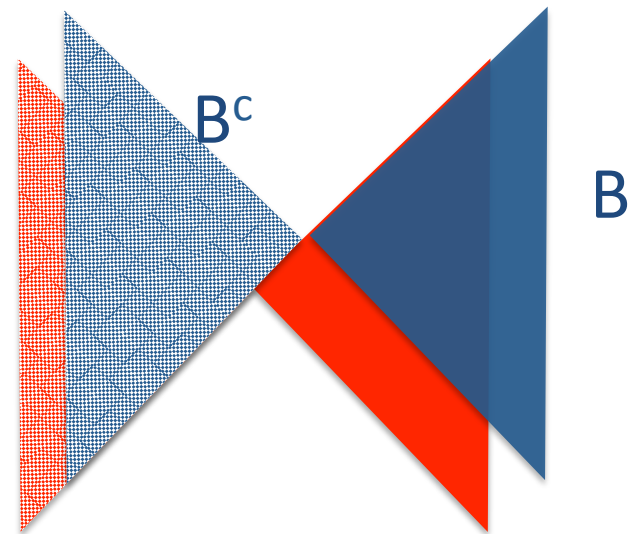
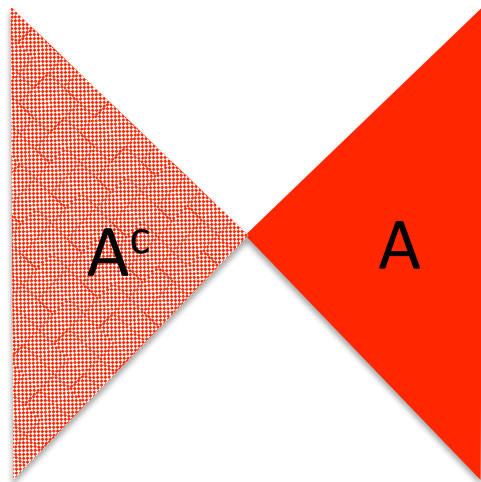
Idea of the argument



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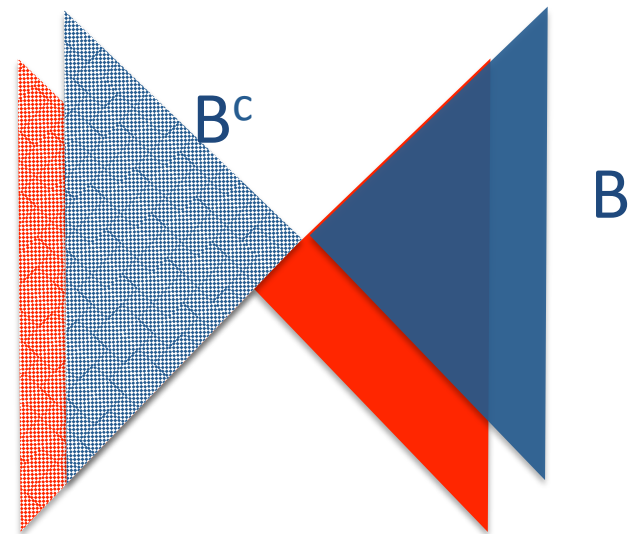
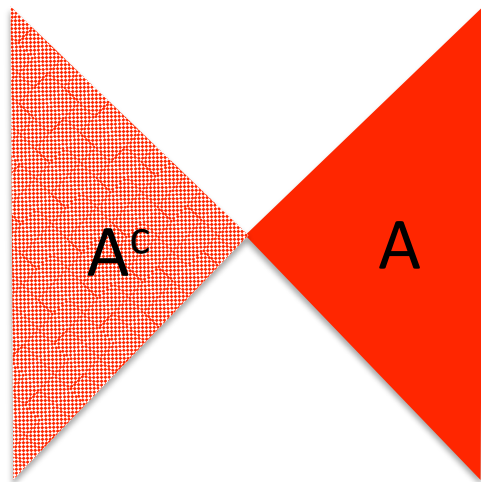


Idea of the argument



$$\begin{array}{l} B \subset A \\ A^c \subset B^c \end{array} \longrightarrow \begin{array}{l} S(\rho_B, \sigma_B) \leq S(\rho_A, \sigma_A) \\ S(\rho_{A^c} | \sigma_{A^c}) \leq S(\rho_{B^c} | \sigma_{B^c}) \end{array}$$

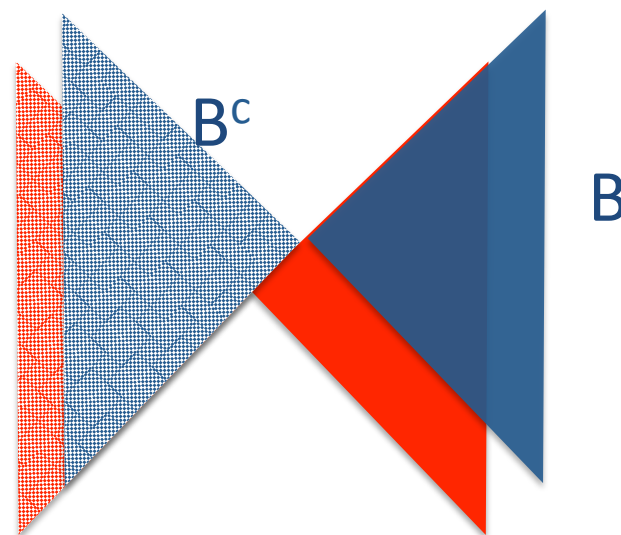
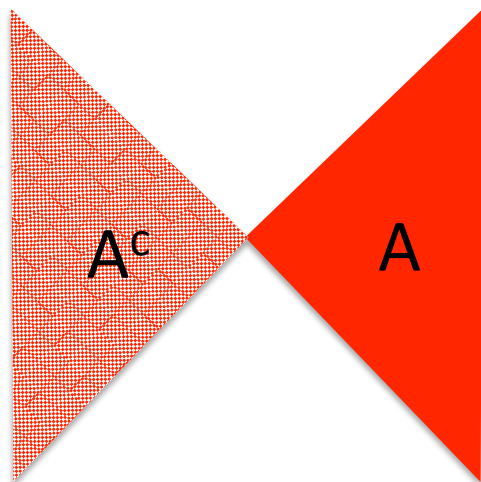
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$$\longrightarrow \langle K_B \rangle - \langle K_{B^c} \rangle \leq \langle K_A \rangle - \langle K_{A^c} \rangle$$

Idea of the argument



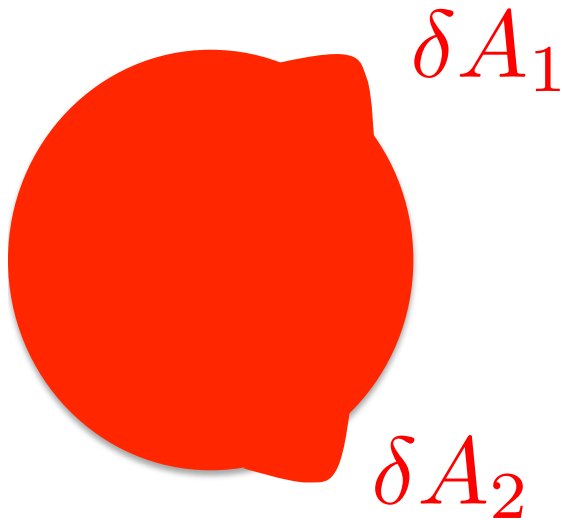
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$$\longrightarrow \langle K_B \rangle - \langle K_{B^c} \rangle \leq \langle K_A \rangle - \langle K_{A^c} \rangle$$

$$\longrightarrow 0 \leq \langle B_A \rangle - \langle B_B \rangle = -\langle P_+ \rangle \Delta X^+$$

Real arguments uses...

Shape dependence of the entropy



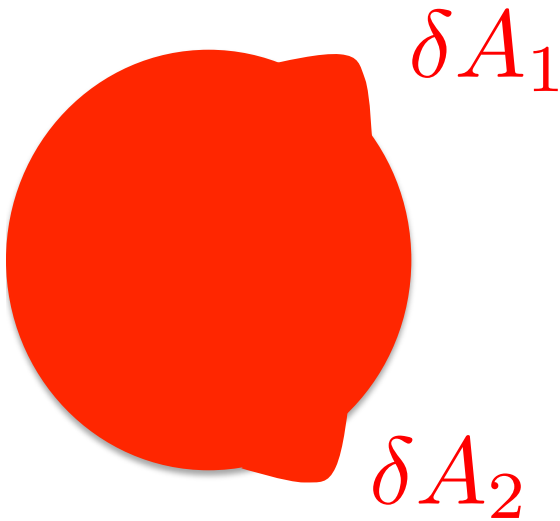
Small deformation from a spherical surface.

Leading quadratic dependence on the deformation:

Faulkner, Leigh, Parrikar

Nozaki, Numasawa, Prudenziati, Takayanagi, Miao, Witczak-Krempa, Bueno, Myers, Rosenhaus, Smolkin, Mezei, Allais, Bianchi, Meineri, Balakrishnan, Dutta, Carmi, Lewkowycz, Perlmutter, Lee, McGough, Safdi, Dowker, Chapman, Bianchi, Galante, Bhattacharya, Hubeny, Rangamani, Czech, Lamprou, McCandish, Sully, Klebanov, Pufu, Nishioka, Elvang, Hadjiantonis, Fonda, Seminara, Tonni...

Shape dependence of the entropy



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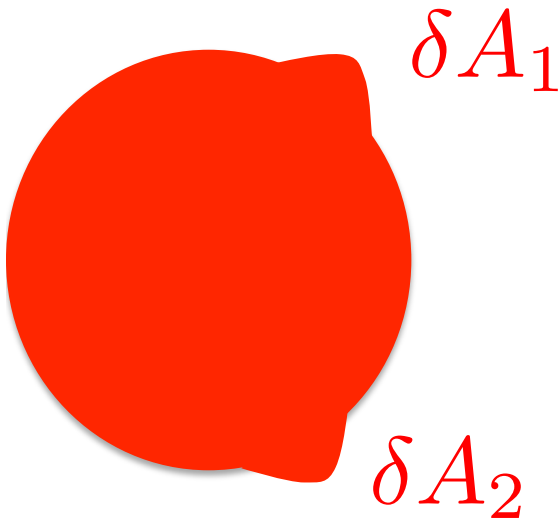
Fixed by conformal symmetry and C_T , the vacuum two point function of the stress tensor.

Idea: Changing shape \rightarrow changing metric \rightarrow
insertions of stress tensor

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Shape dependence of the entropy



δA_1

Small deformation from a spherical surface.

Leading quadratic dependence on the deformation:

Fixed by conformal symmetry and C_T , the vacuum two point function of the stress tensor.

δA_2

Idea: Changing shape \rightarrow changing metric \rightarrow
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Faulkner, Leigh, Parrikar

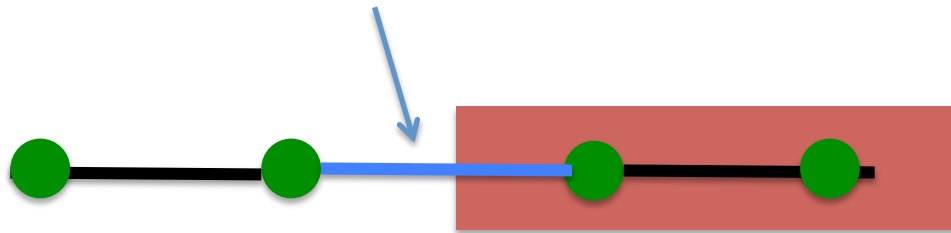
Universality of corner entropy.

Nozaki, Numasawa, Prudenziati, Takayanagi, Miao, Witczak-Krempa, Bueno, Myers, Rosenhaus, Smolkin, Mezei, Allais, Bianchi, Meineri, Balakrishnan, Dutta, Carmi, Lewkowycz, Perlmutter, Lee, McGough, Safdi, Dowker, Chapman, Bianchi, Galante, Bhattacharya, Hubeny, Rangamani, Czech, Lamprou, McCandish, Sully, Klebanov, Pufu, Nishioka, Elvang, Hadjiantonis, Fonda, Seminara, Tonni...

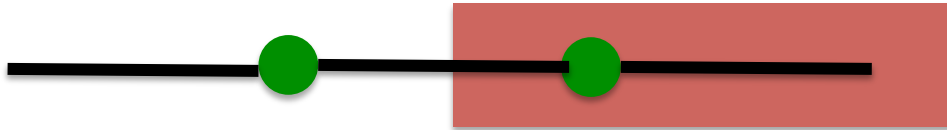
Gauge fields and Edge Modes



Center variables = Electric field on the separating surface.



Gauge fields and Edge Modes



Donnelly Wall Radicevic
Casini Huerta Rosabal
Hawking, Strominger, Perry
Harlow

$$H = \sum_q H_L^q \times H_R^{-q}$$

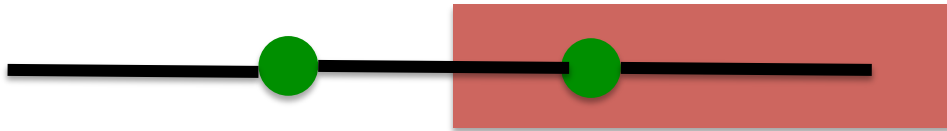
Splitting of Hilbert space in each charge sector.

Shannon term

$$\rho \rightarrow p_q, \rho_q, \quad S = \sum_q -p_q \text{Tr}[\rho_q \log \rho_q] - p_q \log p_q$$

↓

Gauge fields and Edge Modes



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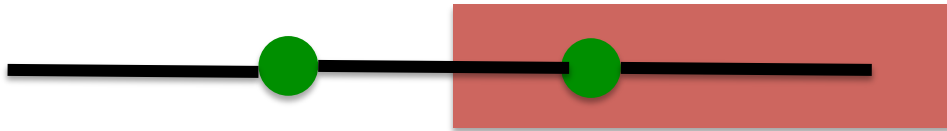
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Donnelly Freidel

Expect a similar story for gravity: Electric field \rightarrow geometry of the surface

Gauge fields and Edge Modes



Donnelly Wall Radicevic
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↓

Consequences of this for UV finite quantities remain to be seen...

Quantum entropy in semiclassical gravity

Results in semiclassical gravity

- QFT in a gravitational background.

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- Corrections to black hole entropy. BPS, non BPS...

See eg. Sen et al

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$$S_{gen} = \frac{\text{Area}}{4G_N} + S_{ent}$$

Bombelli, Koul, Lee, Sorkin
Srednicki

Callan Wilzcek Larsen Holzhey
Susskind Uglum

Solodhukin, Frolov, Fursaev ...

UV finite

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UV finite

- Second law of thermodynamics, S increases
(monotonicity of relative entropy)

Hawking, Wall

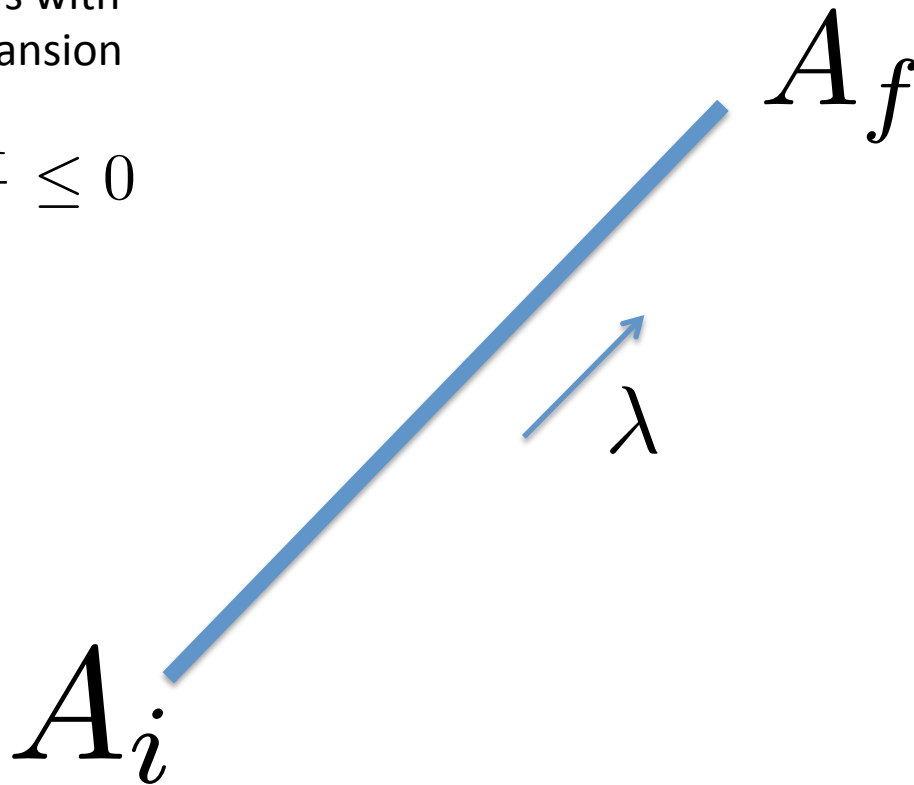
Results in semiclassical gravity

- Better understanding of the quantum Bousso bound.

Classical Bousso bound

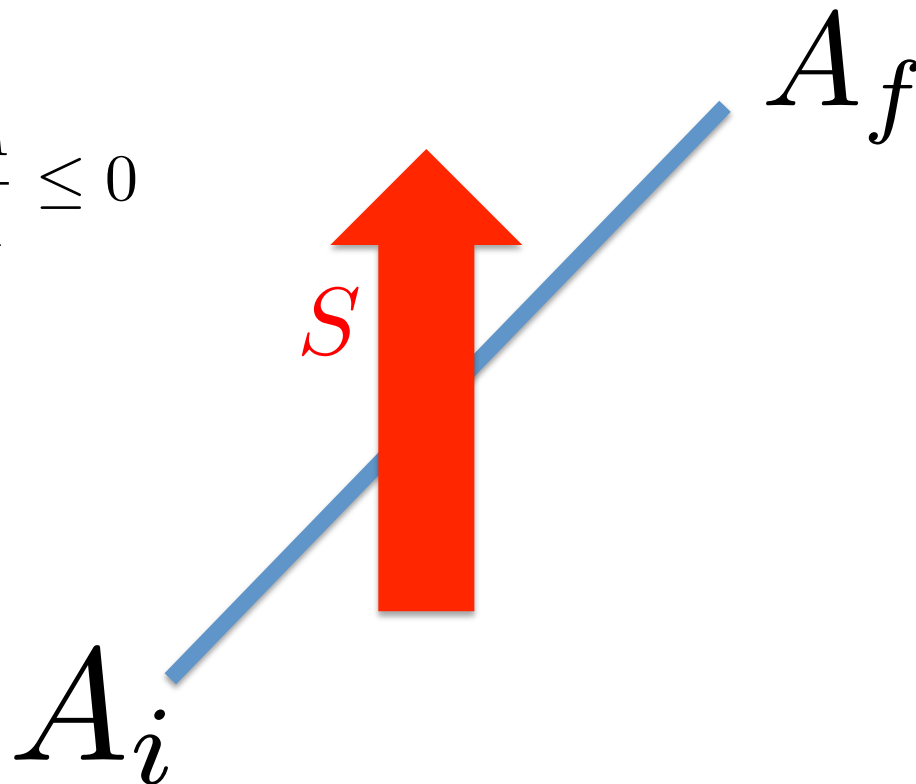
Set of null rays with
negative expansion

$$\theta = \frac{1}{A} \frac{dA}{d\lambda} \leq 0$$



Classical Bousso bound

$$\theta = \frac{1}{A} \frac{dA}{d\lambda} \leq 0$$



$$S \leq \frac{A_i - A_f}{4G_N}$$

Bousso
Flanagan, Marolf, Wald

Quantum Bousso Bound

- 2 versions

1) Bousso, Casini, Fischer, JM

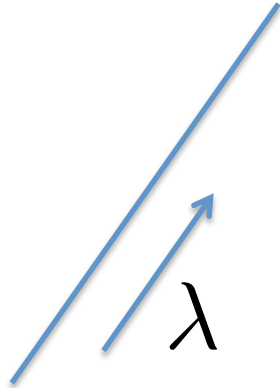
2) Strominger, Thompson
Bousso, Fischer, Leichenauer,
Wall + Koeller

Quantum Bousso Bound

- Quantum focusing conjecture

Strominger, Thompson
Bousso, Fischer, Leichenauer,
Wall + Koeller

- Classical focusing theorem



$$\theta \equiv \frac{1}{A} \frac{dA}{d\lambda}$$

$$\frac{d\theta}{d\lambda} \leq 0, \quad \text{since} \quad T_{\lambda\lambda} \geq 0$$

Quantum Focusing conjecture

- Define the “quantum expansion”

$$\Theta \equiv \frac{1}{A} \frac{dS_{gen}}{d\lambda}$$

Bousso, Fischer, Leichenauer,
Wall + Koeller

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Bousso, Fischer, Leichenauer,
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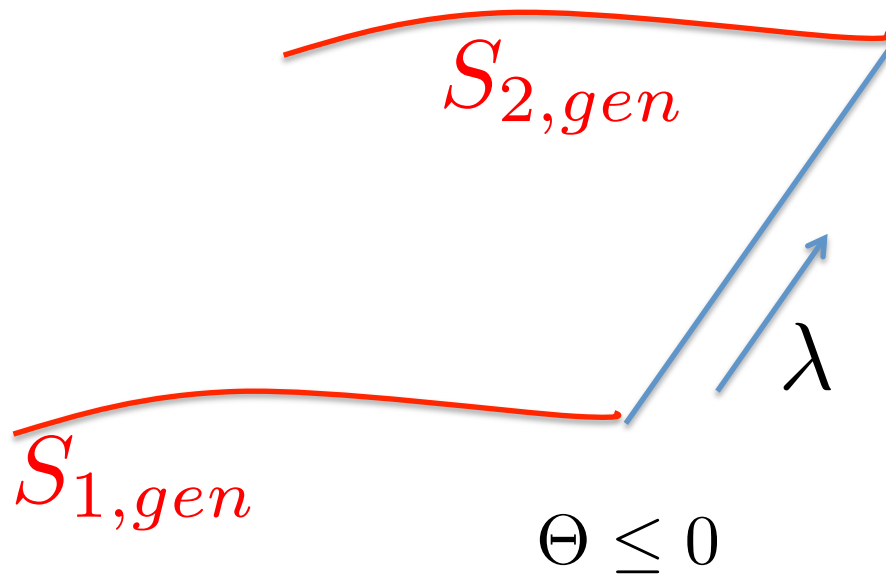


- Conjecture

$$\frac{d\Theta}{d\lambda} \leq 0$$

Quantum Focusing conjecture

Bousso, Fischer, Leichenauer,
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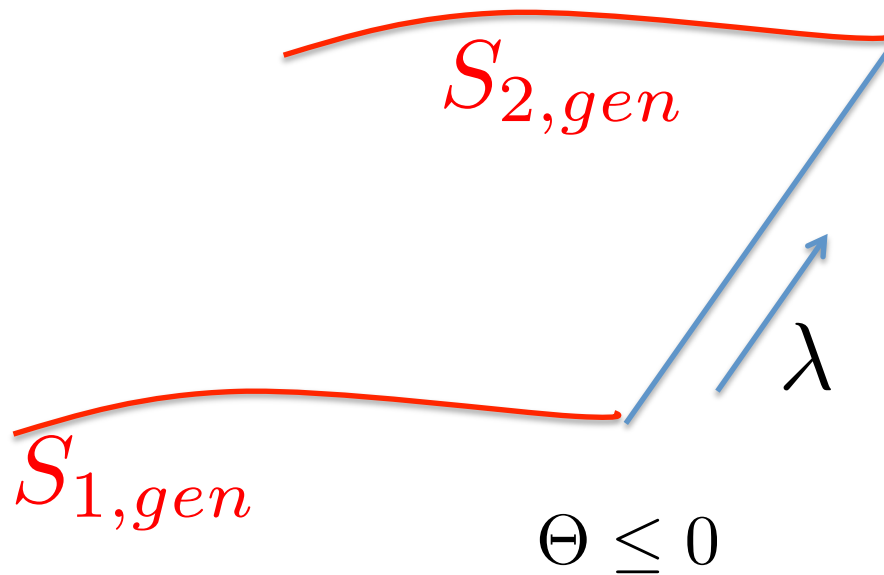


$$\Rightarrow \Delta S \leq \frac{\Delta A}{4G_N}$$

Classical Bousso bound

Quantum Focusing conjecture

Bousso, Fischer, Leichenauer,
Wall + Koeller



$$\Rightarrow \Delta S \leq \frac{\Delta A}{4G_N}$$

Classical Bousso bound

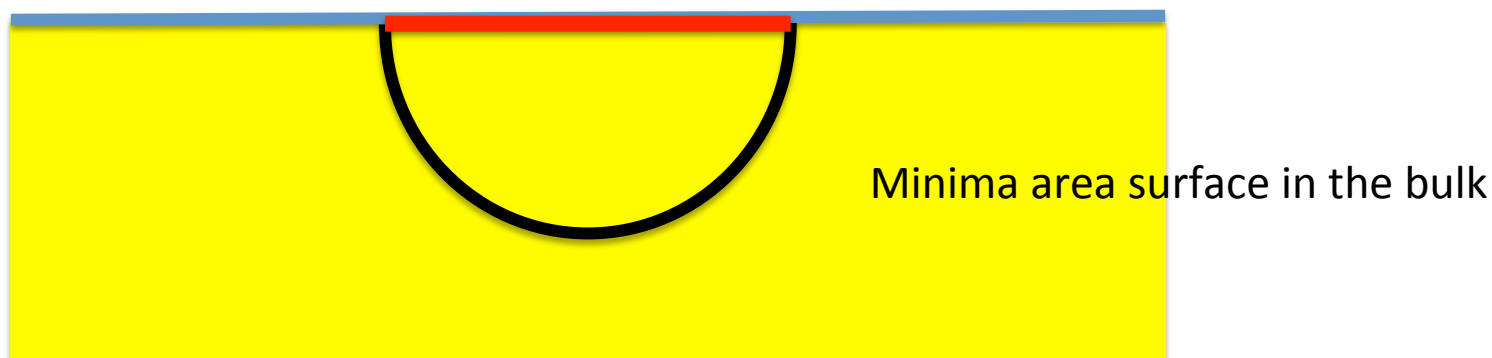
Weak gravity:

$$\langle T_{--} \rangle \geq \frac{1}{2\pi} \lim_{A \rightarrow 0} \frac{S''_{out}}{A}$$

Quantum null energy condition. Proven in some cases.

Entanglement and holography

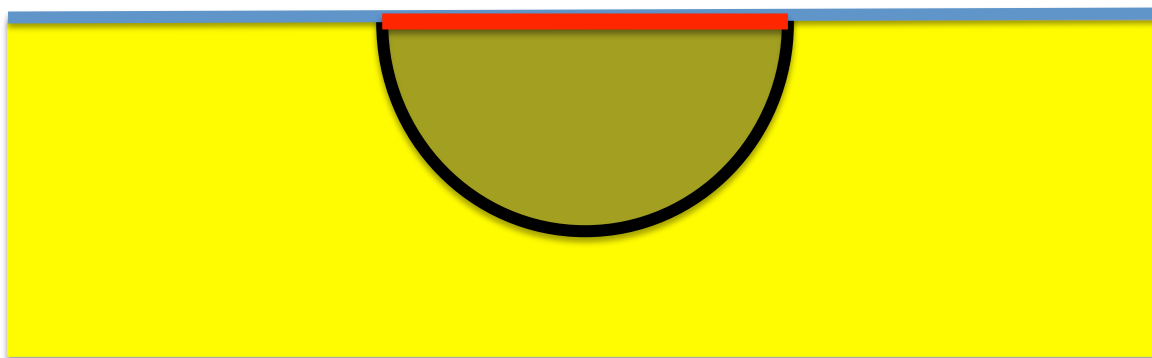
Entanglement in theories with gravity duals



$$S = \frac{(\text{Area})_{\min}}{4G_N}$$

Ryu Takayanagi
Hubeny, Rangamani, Takayangi

Entanglement in theories with gravity duals



$$S = \frac{(\text{Area})_{\min} + \alpha'(\text{curvature}) + \dots}{4G_N} + S_{\text{bulk}} + o(G_N)$$

Wald, Myers, Jacobson, ... ,Dong

Faulkner, Lewkowicz, JM
Barrella, Dong, Hartnoll, Martin

Relative entropy

Lashkari, Van Raamsdonk
Jafferis, Lewkowycz, JM, Suh

$$S(\rho, \sigma) = S_{\text{bulk}}(\rho, \sigma)$$

$$K = \frac{A}{4G_N} + K_{\text{bulk}}$$

Relative entropy

Lashkari, Van Raamsdonk
Jafferis, Lewkowycz, JM, Suh

$$S(\rho, \sigma) = S_{\text{bulk}}(\rho, \sigma)$$

$$K = \frac{A}{4G_N} + K_{\text{bulk}}$$

Two points of view:

1- Only holds for restricted semiclassical states...

2 -All dof are visible in the bulk (cutoff independent indication that all of black hole entropy comes from the atmosphere)

Qualitative idea for black hole entropy

$$S_{gen} = \frac{\text{Area}}{4G_N} + S_{ent}$$

As $\epsilon \rightarrow 0$, area term goes to zero and all entropy is entanglement.

Is all of black hole entropy just bulk entanglement entropy, with a suitable cutoff?

This happens in “induced gravity theories” (not well defined)...

Conservative : do not mix the leading order with the subleading order...

Dreamer: figure out in what sense this is true....

$$S(\rho, \sigma) = S_{\text{bulk}}(\rho, \sigma)$$

Is a cutoff independent indication of this.

Einstein equations from the entanglement formula

Initially

Ryu-Takayanagi
formula



Einstein's
equations

Einstein equations from the entanglement formula

Can go in the other direction

Ryu-Takayanagi
formula



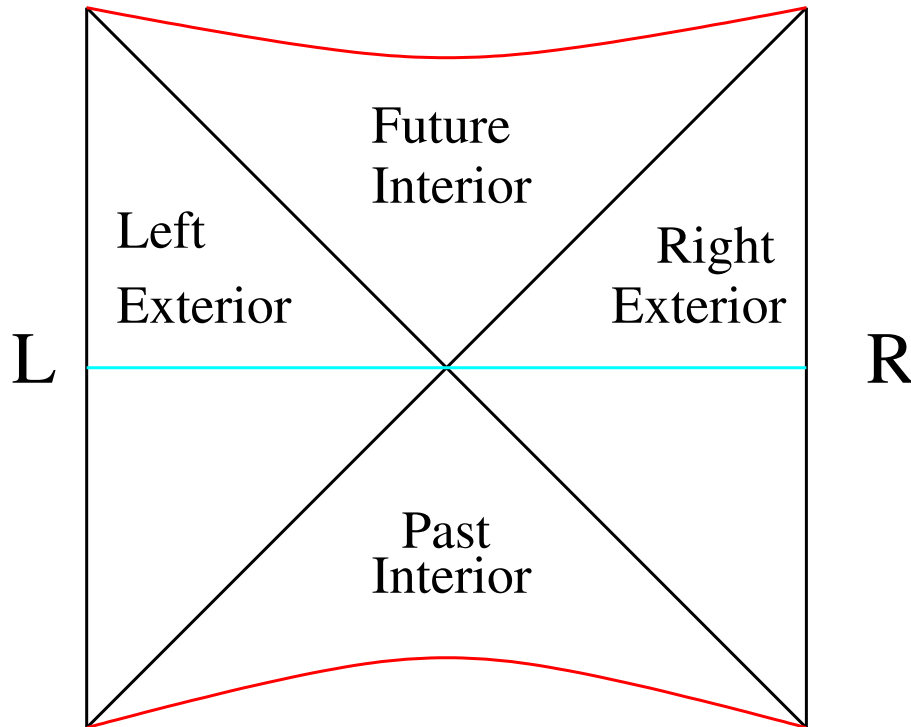
Einstein's
equations

Lashkari, McDermott, Van Raamsdonk, Faulkner,
Guica, Hartman, Myers, Swingle
Jacobson

(not in full generality yet...)

Wormholes

Wormholes and entangled states



Full Schwarzschild-AdS
Geometry

=

Entangled state in
two non-interacting
CFT's.

Israel
JM

$$|\Psi\rangle = \sum_n e^{-\beta E_n/2} |E_n\rangle_L^{CPT} \times |E_n\rangle_R$$

Wormhole physics

- Integrated null energy condition \rightarrow no signal propagation. (recall recent entanglement based proof)

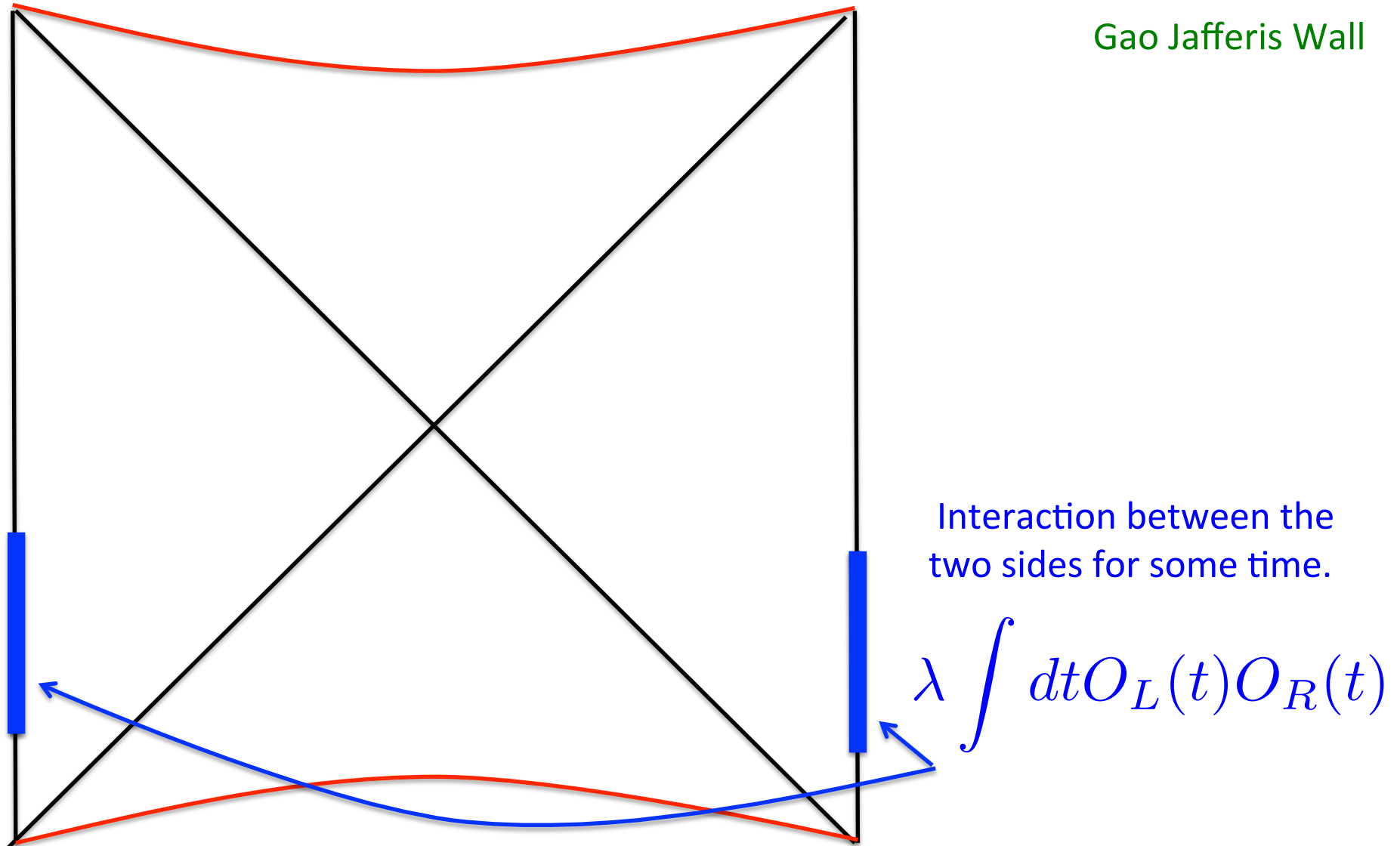
Wormhole physics

- Integrated null energy condition \rightarrow no signal propagation. (recall recent entanglement based proof)
- Allowing interactions between the two sides \rightarrow can have negative energy \rightarrow can get signal propagation.

Gao Jafferis Wall

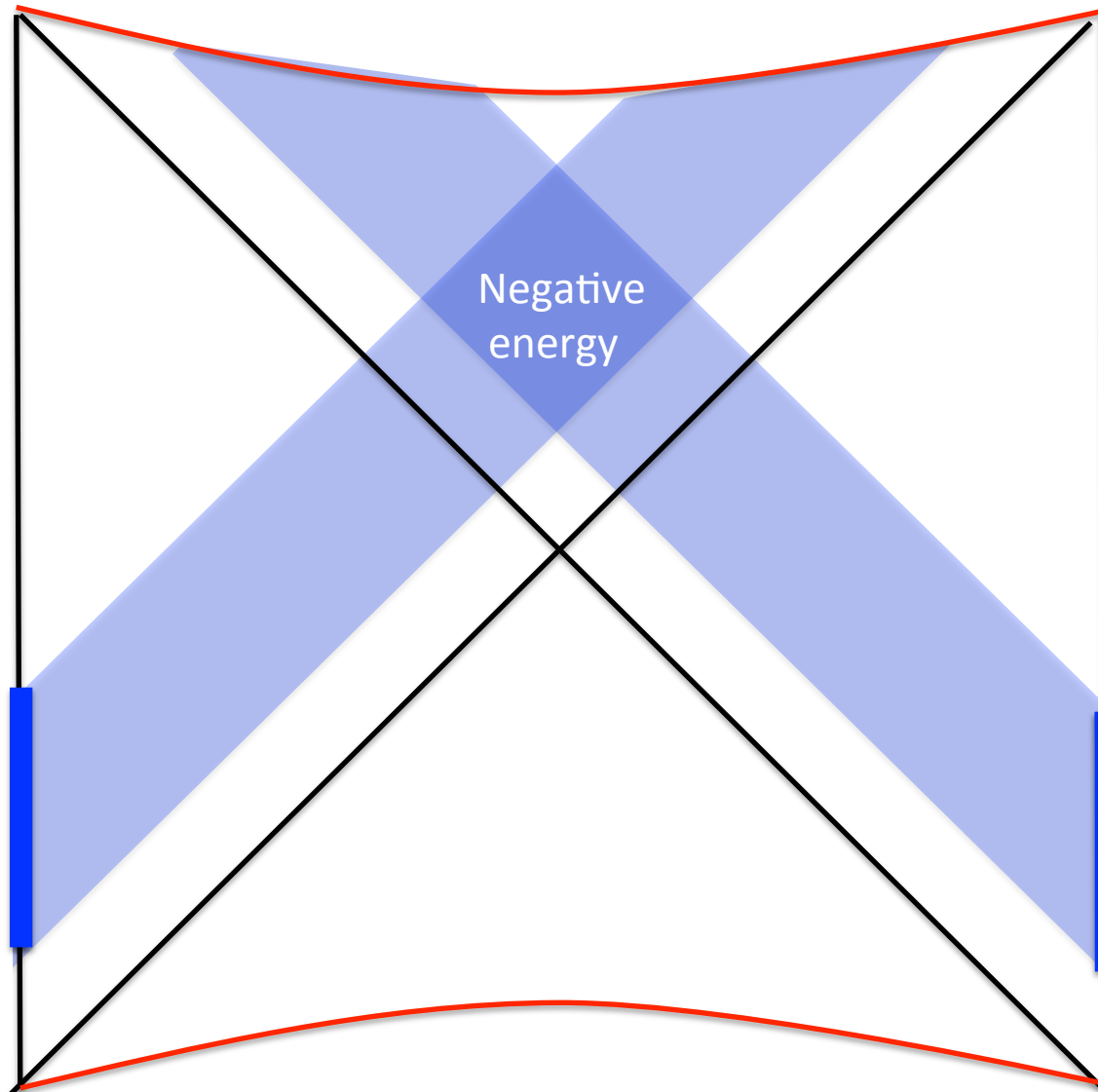
Wormholes and entangled states

Gao Jafferis Wall



Wormholes and entangled states

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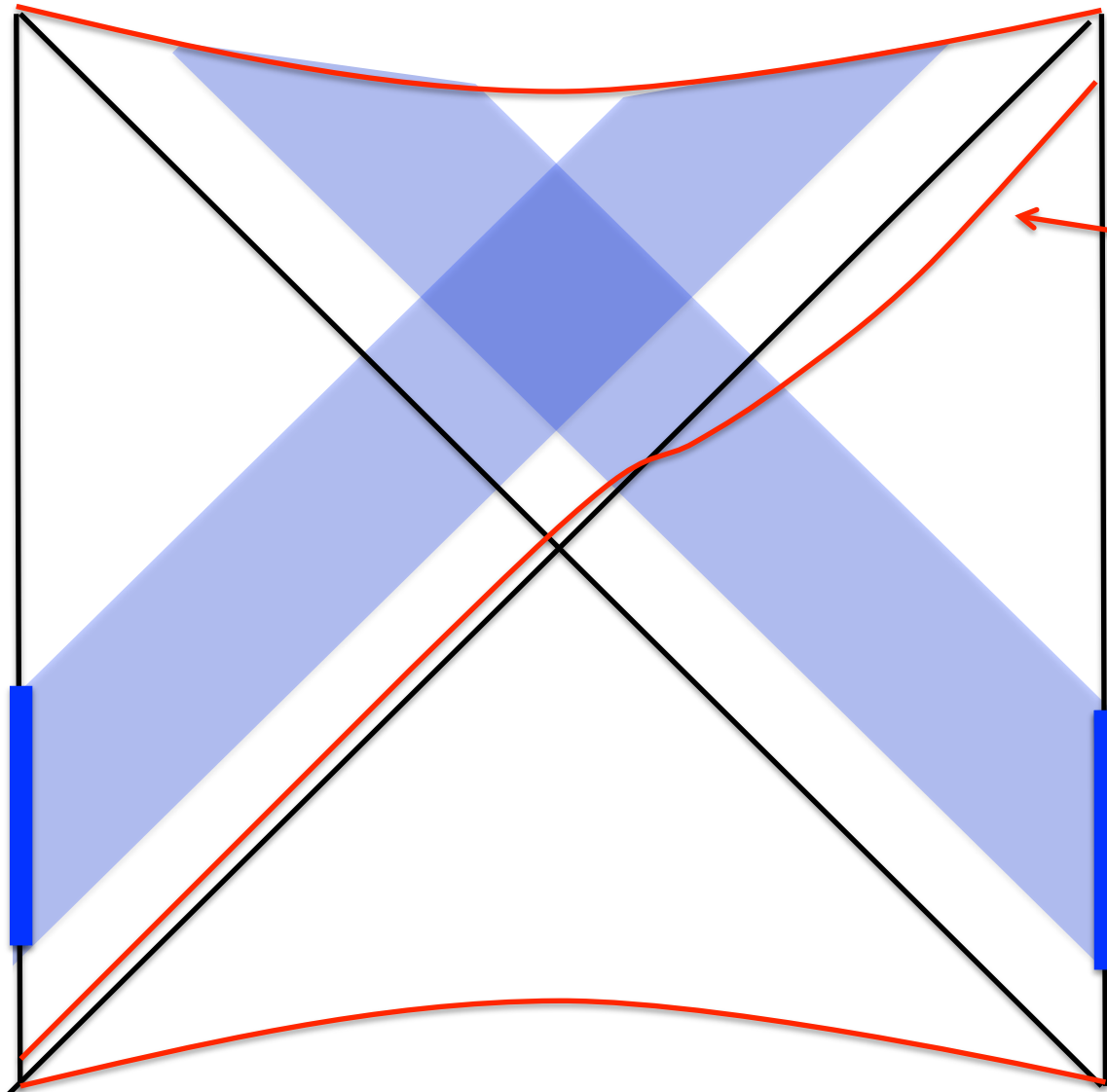


Interaction between the two sides for some time.

$$\lambda \int dt O_L(t) O_R(t)$$

Wormholes and entangled states

Gao Jafferis



Signal through
the wormhole

Interaction between the
two sides for some time.

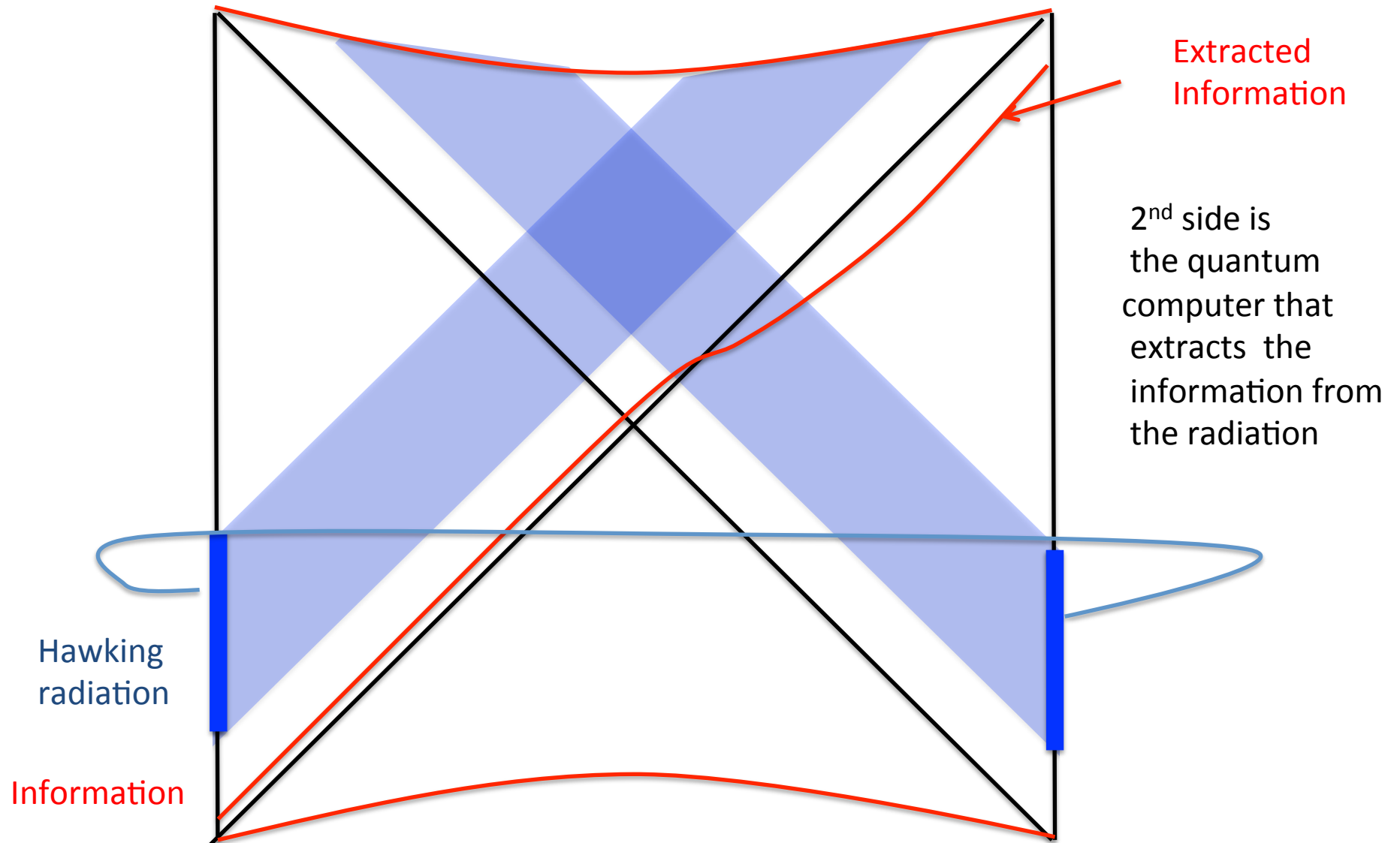
$$\lambda \int dt O_L(t) O_R(t)$$

- Connected with “black holes as mirrors”

Hayden Preskill

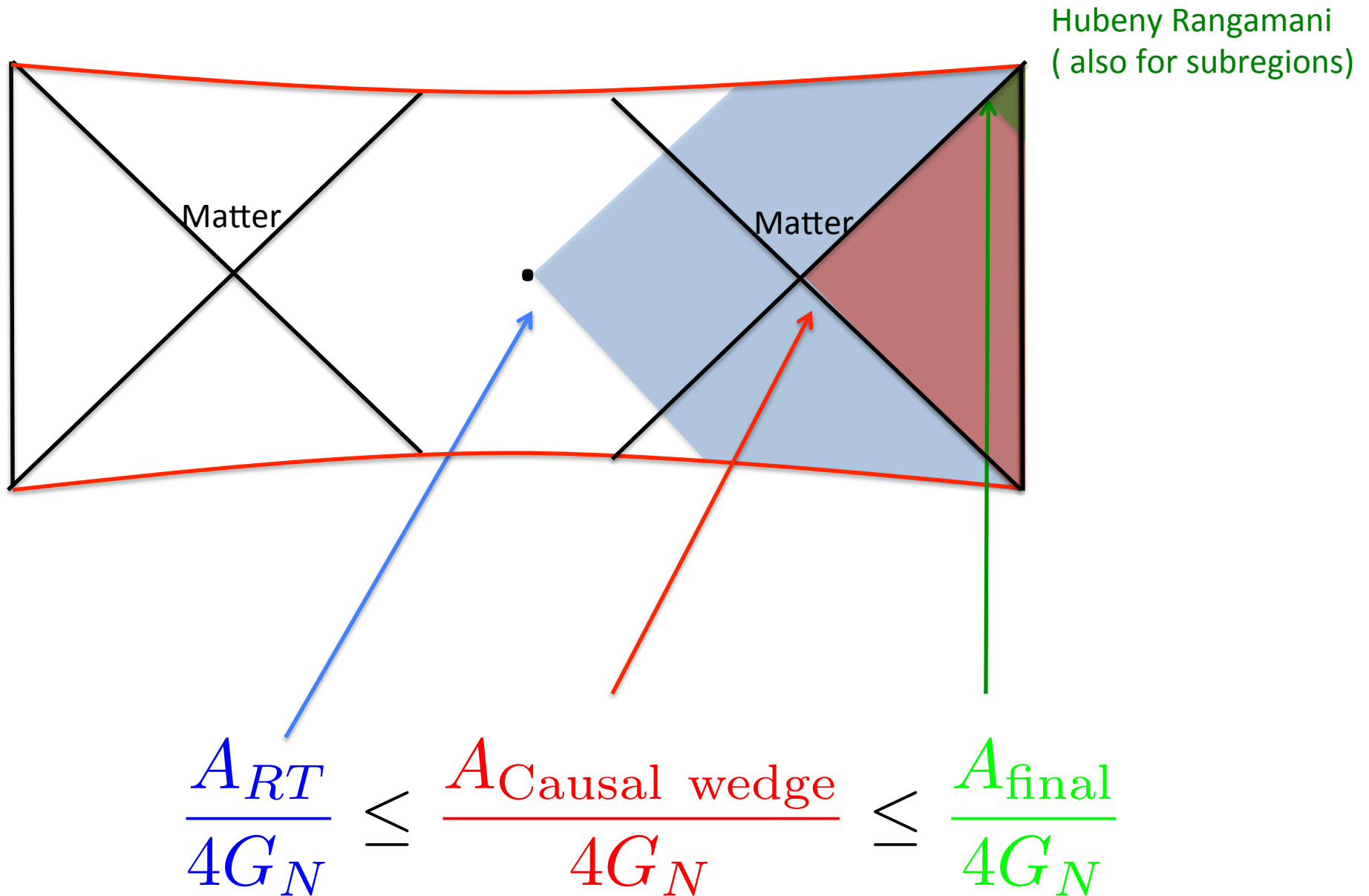
- If one has access to a state that is maximally entangled with a black hole, then information that is sent into the black hole can be recovered by looking at a small amount of Hawking radiation.

Wormholes and entangled states

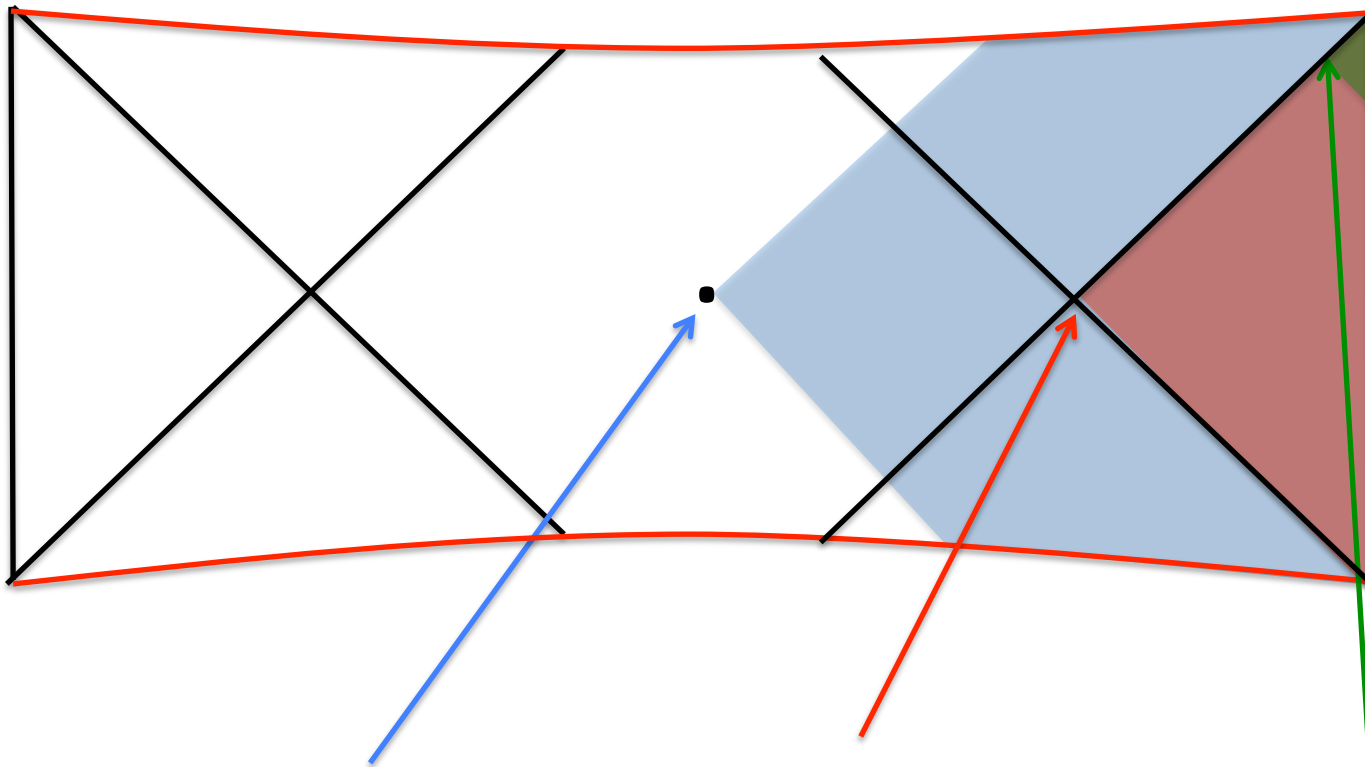


Not just entanglement entropy...

Entanglement wedge vs. causal wedge



Entanglement wedge vs. causal wedge



$$\frac{A_{RT}}{4G_N} + S_{bulk} \leq \frac{A_{\text{Causal wedge}}}{4G_N} + S_{bulk} \leq \frac{A_{\text{final}}}{4G_N} + S_{bulk}$$

2nd Law


Different notions of entropy

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Fine grained entropy

These should be coarse grained entropies

Different notions of entropy

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Fine grained entropy

These should be coarse grained entropies

Restrict the algebra of observables to gravity fields. Simple operators acting within a scrambling time

Entropy of the maximal entropy state compatible with the density matrix of the simple algebra...

Kelly, Wall, Papadodimas, Raju,....

Tensor Networks

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- Method to write wavefunctions. Ansatz for the wavefunction.

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- Wavefunction constructed out of simpler objects, out of simpler tensors.
- Originated as a numerical method.
- They embody the renormalization group.
- There are some qualitative similarities with gravity.

Examples

- Matrix product states.

white

$$\Psi(s_1, s_2, \dots, s_N) = \text{Tr}[T_{s_1} T_{s_2} \cdots T_{s_n}]$$

$$T_{s_i} = (T_{s_i})_l^k \quad D \times D \quad \text{matrix}$$

Examples

- Matrix product states.

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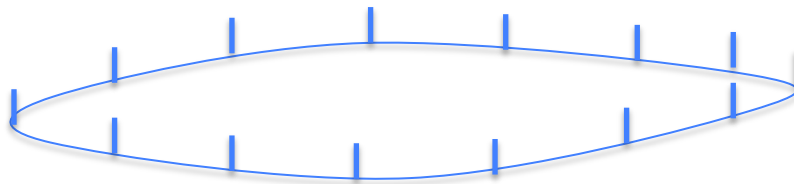
$$\Psi(s_1, s_2, \dots, s_N) = \text{Tr}[T_{s_1} T_{s_2} \cdots T_{s_N}]$$

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$$2D^2, \quad \text{or} \quad 2ND^2 \ll 2^N$$

Subspace of the
Hilbert space !

Works for states with finite
Amount of long range
entanglement



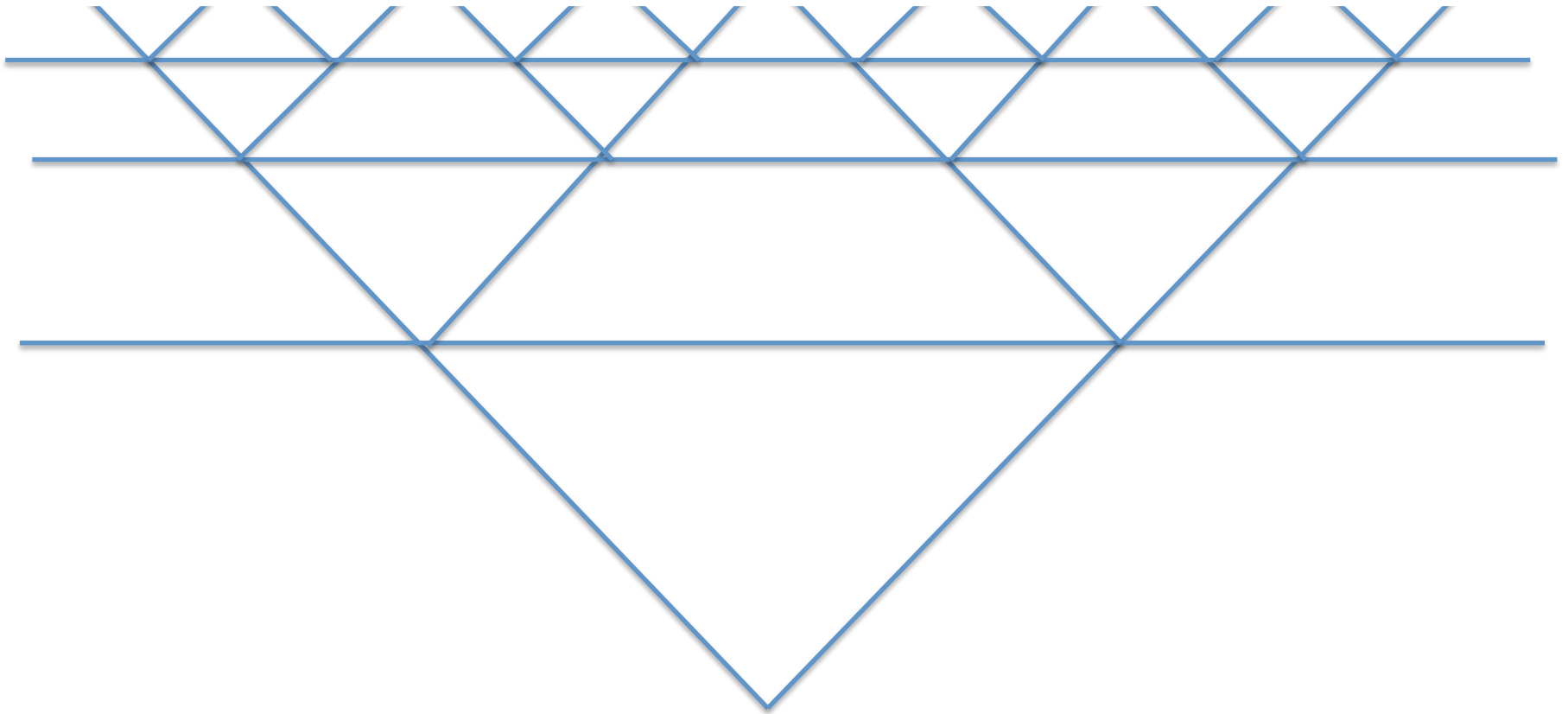
Vertex = tensor

Open line = open index

Link = contracted index

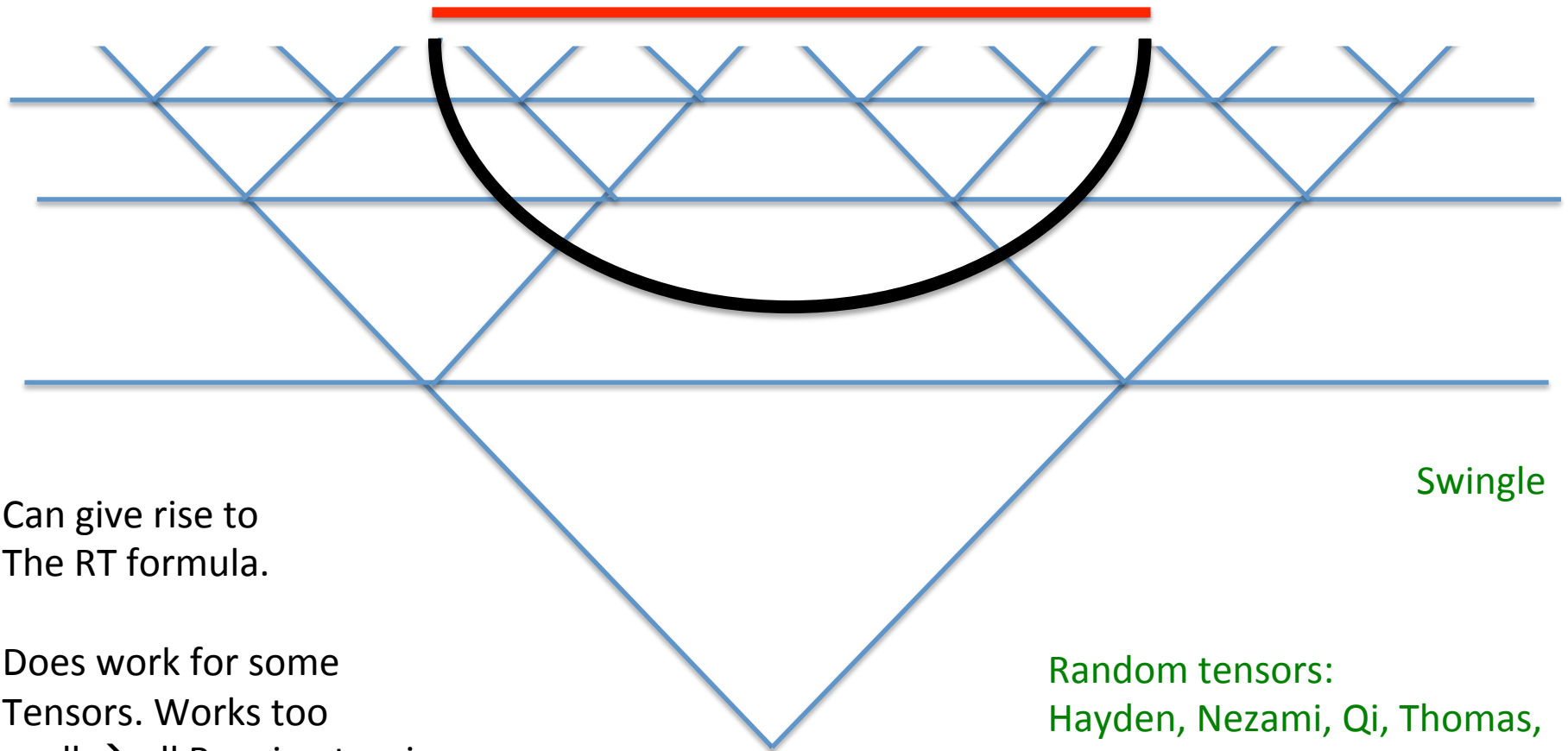
Scale invariant wavefunctions

Vidal



Each vertex is a five index tensor. Each line is an index contraction.

Scale invariant wavefunctions

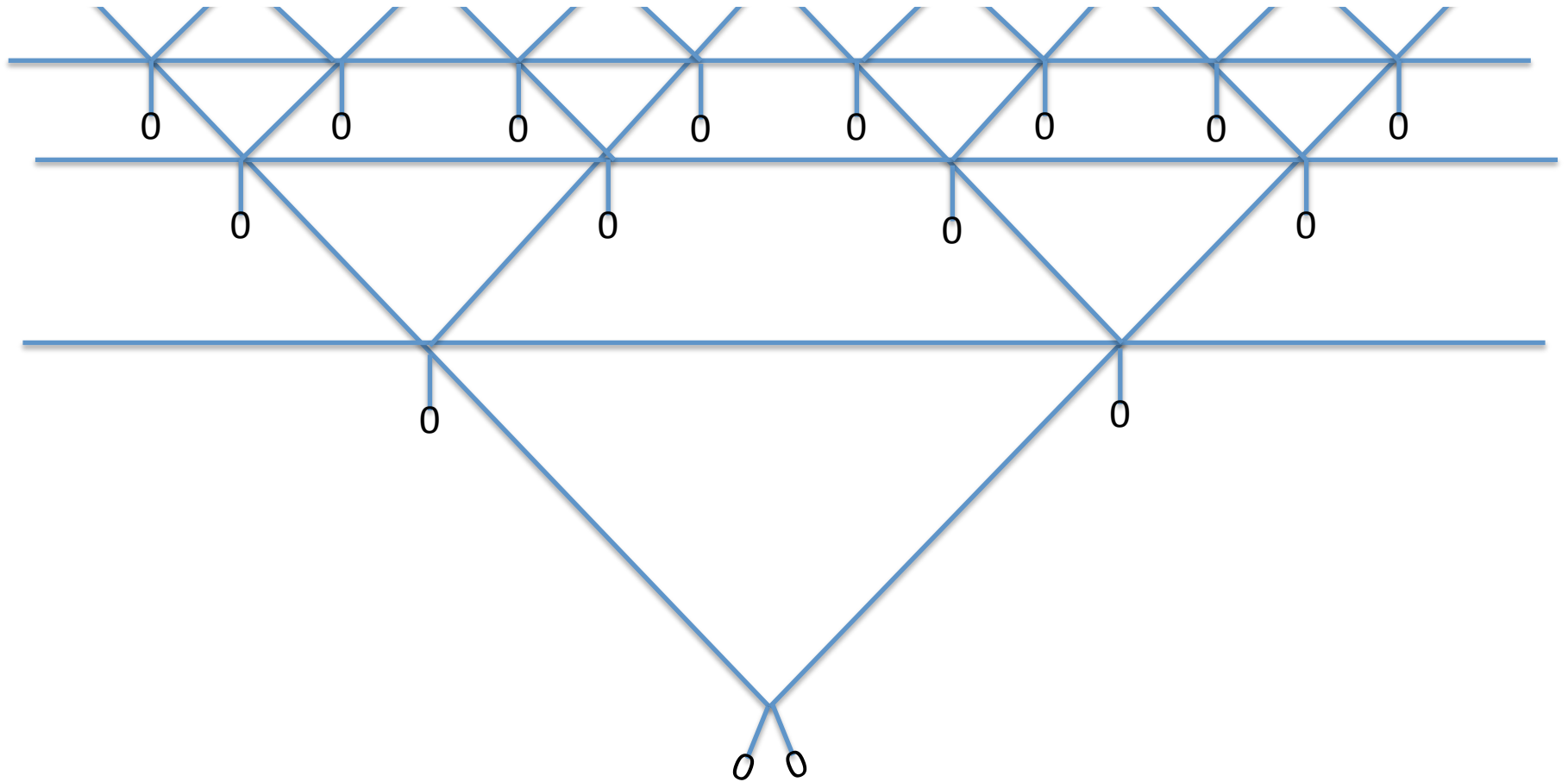


Can give rise to
The RT formula.

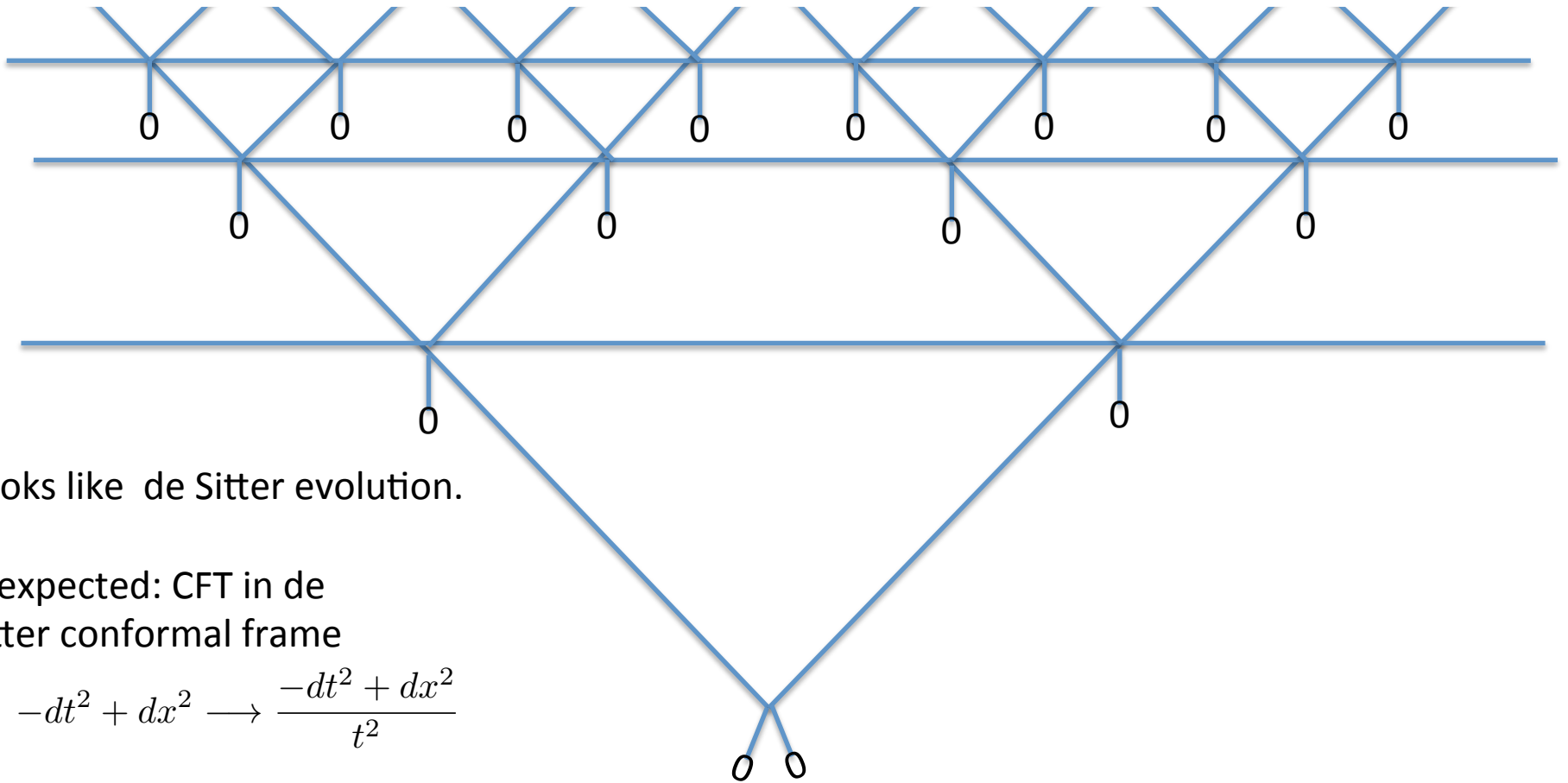
Does work for some
Tensors. Works too
well \rightarrow all Renyi entropies

Random tensors:
Hayden, Nezami, Qi, Thomas,
Walter, Yang

Qualitatively similar to the bulk in AdS/CFT



As a unitary transformation



Looks like de Sitter evolution.

Is expected: CFT in de Sitter conformal frame

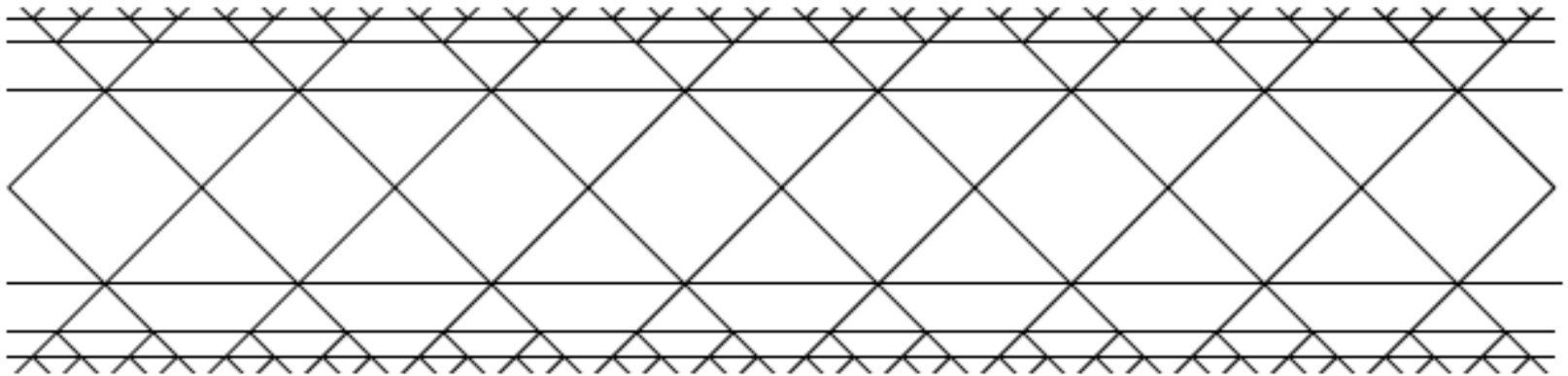
$$-dt^2 + dx^2 \longrightarrow \frac{-dt^2 + dx^2}{t^2}$$

Connection to “kinematic space” (space of pairs of points) Czech, Lamprou, McCandish, Sully

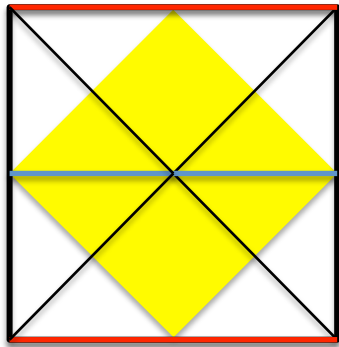
Could also use it as a representation of the cosmological wavefunction...

Peeking into the interior

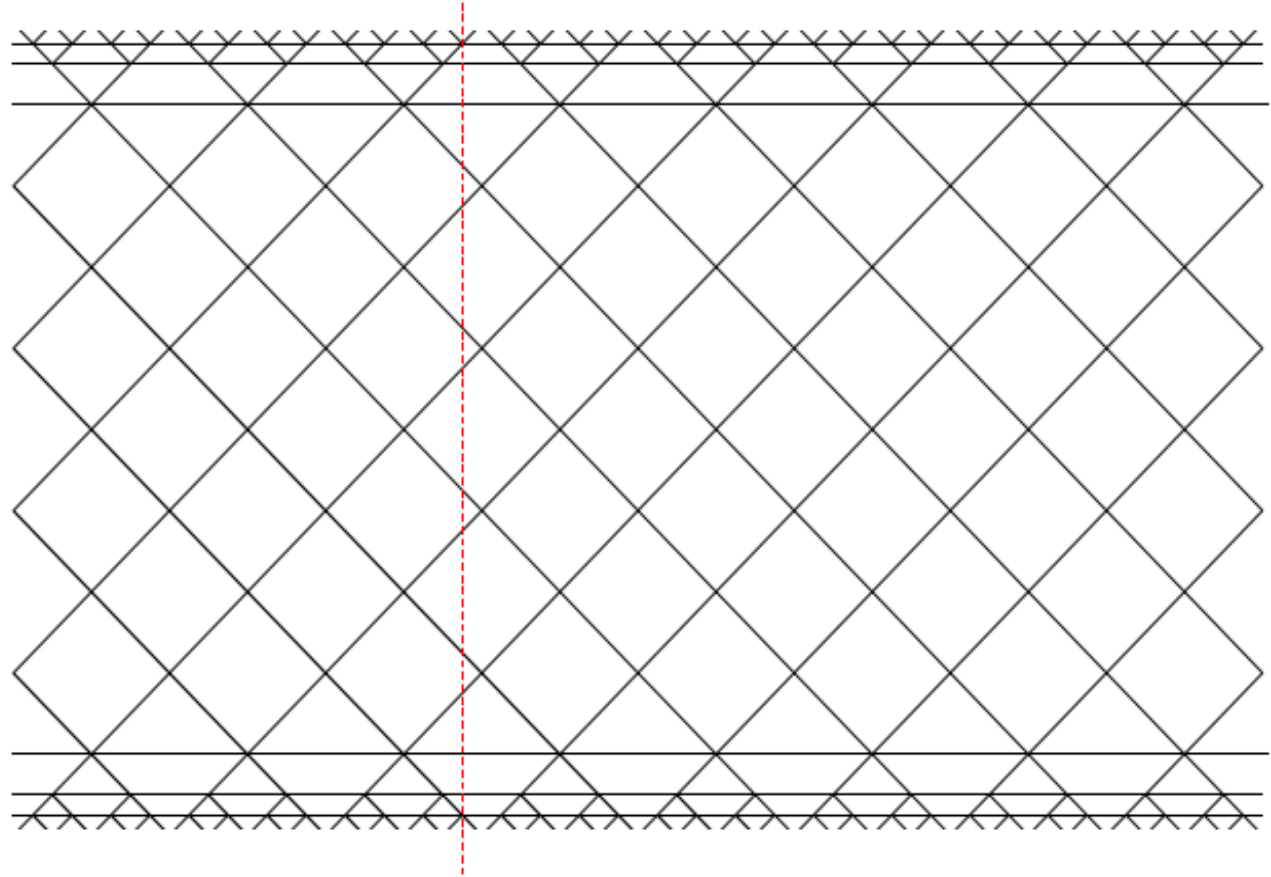
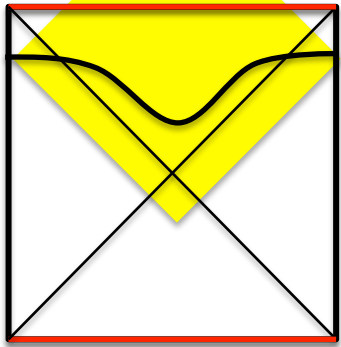
Thermal states



→
Spatial direction along horizon



Time evolution of thermofield double



Similar to the stretching of the geometry behind the horizon.

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- View network as preparing the state by simple operations from a simple product state.

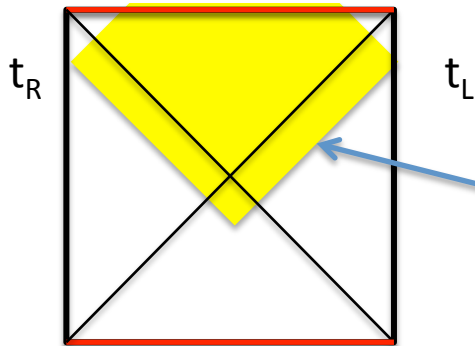
What networks to choose ?

- Choose ``simple'' elementary tensors = small tensors
- View network as preparing the state by simple operations from a simple product state.
- Complexity = number of simple gates

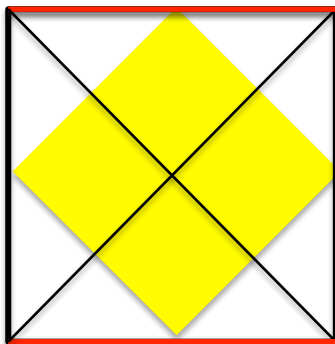
Complexity = Action ?

- Complexity = action of the WdW patch ?

Brown, Roberts, Susskind,
Swingle, Zhao



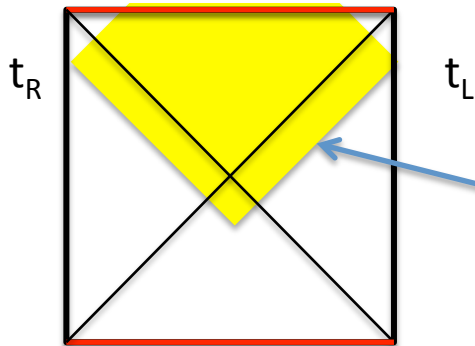
Wheeler de Wit patch



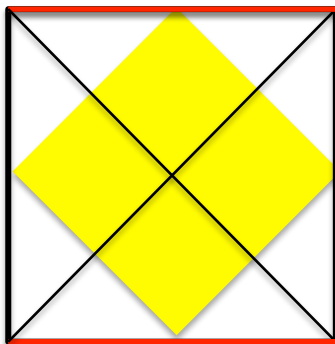
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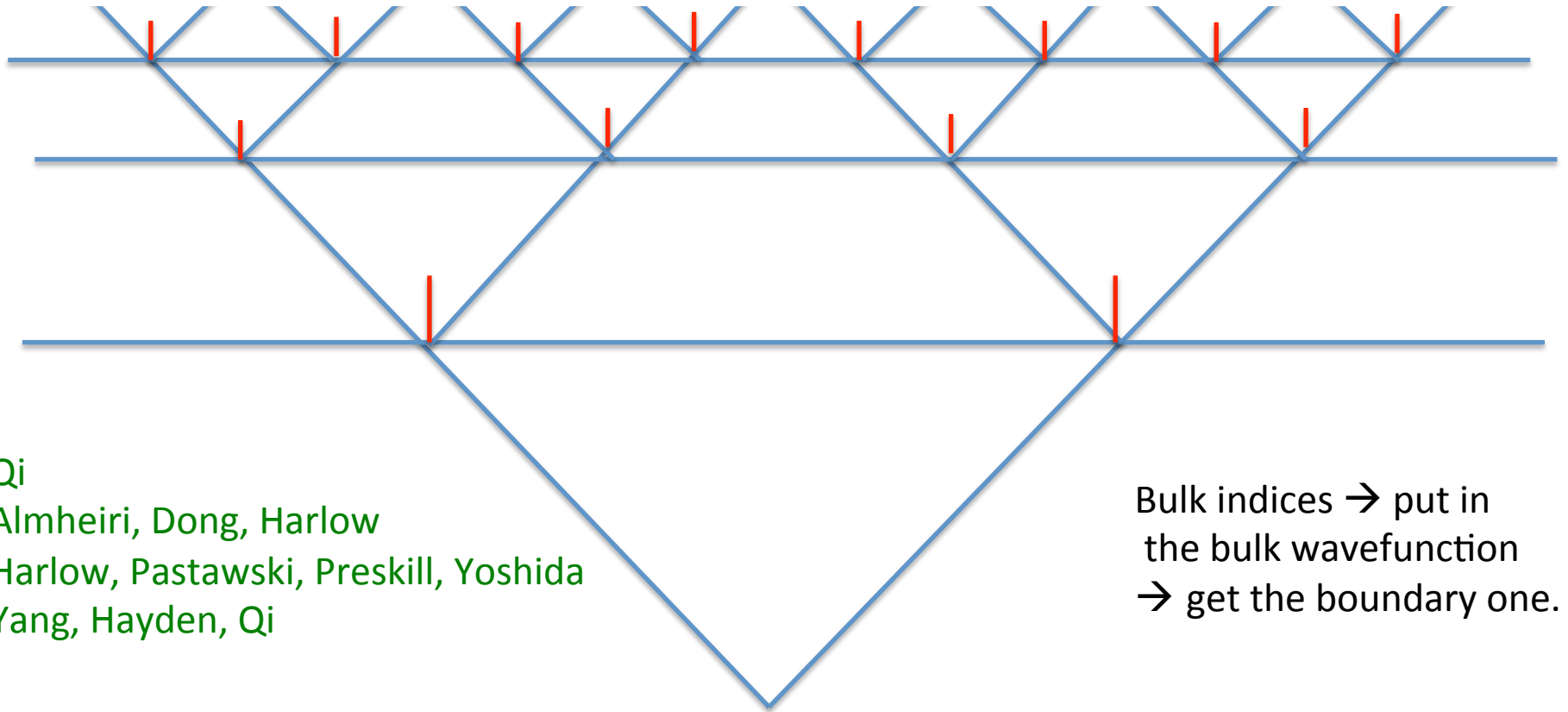


Nice qualitative agreement \rightarrow time dependence

Singularity ?

Other physical interpretation ?

Tensor networks and the holographic encoding



Qi
Almheiri, Dong, Harlow
Harlow, Pastawski, Preskill, Yoshida
Yang, Hayden, Qi

Bulk indices \rightarrow put in
the bulk wavefunction
 \rightarrow get the boundary one.

Tensor network is an encoding of the bulk into the boundary

$$\mathcal{H}_{\text{Bulk}} \longrightarrow \mathcal{H}_{\text{Boundary}}$$

- Capture many qualitative features!
- Local lorentz invariance in the bulk ?

Conclusions

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- Gravity + QFT \rightarrow interesting entropy statements, which are being proved. 2nd Law. Bousso bound. Holographic entanglement formulas...
- Weird wormholes \rightarrow help constrain how spacetime emerges.
- Tensor networks capture interesting properties of black hole geometries. (But not local bulk lorentz invariance, so far...)

End