

# **Information Loss Paradox and Asymptotic Black Holes**

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Kawai et al: [arXiv: 1302.4733]  
[arXiv: 1409.5784]  
[arXiv: 1509.08472]

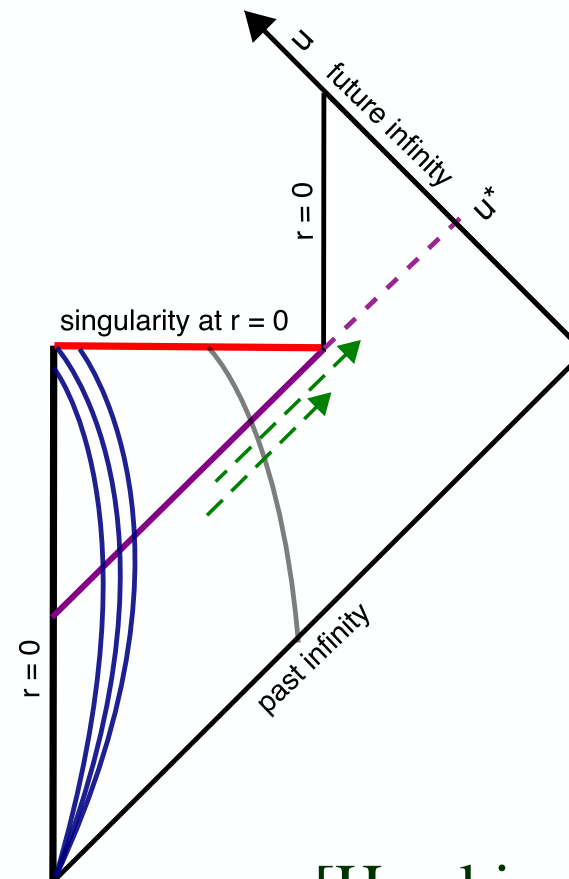
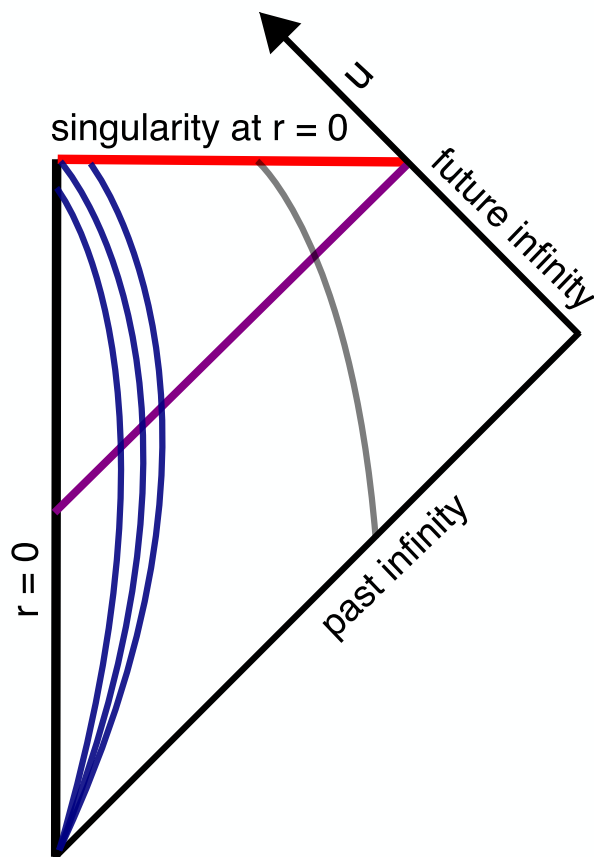
Ho: [arXiv: 1505.02468]  
[arXiv: 1510.07157]  
[arXiv: 160\*.\*\*\*\*\*]

## In the conventional model of BH:

Infalling observer: finite proper time to cross the horizon.

Distant observer: infinite time if no radiation.

Hawking radiation  $\Rightarrow$  Horizon shrinks, but finite time!



[Hawking 1976]

# Misconception #1

For a classical black hole, an infalling object crosses the horizon in finite proper time. This is also true for a very small deformation of the classical black hole, e.g. due to the back-reaction of a very weak radiation.

# Outgoing Vaidya metric

$$ds^2 = - \left( 1 - \frac{a(u)}{r} \right) du^2 - 2du dr + r^2 d\Omega^2$$

$$a(u) = 2M(u) \quad T_{uu} = \frac{G_{uu}}{8\pi G} = -\frac{1}{8\pi G} \frac{\dot{a}(u)}{r^2}$$

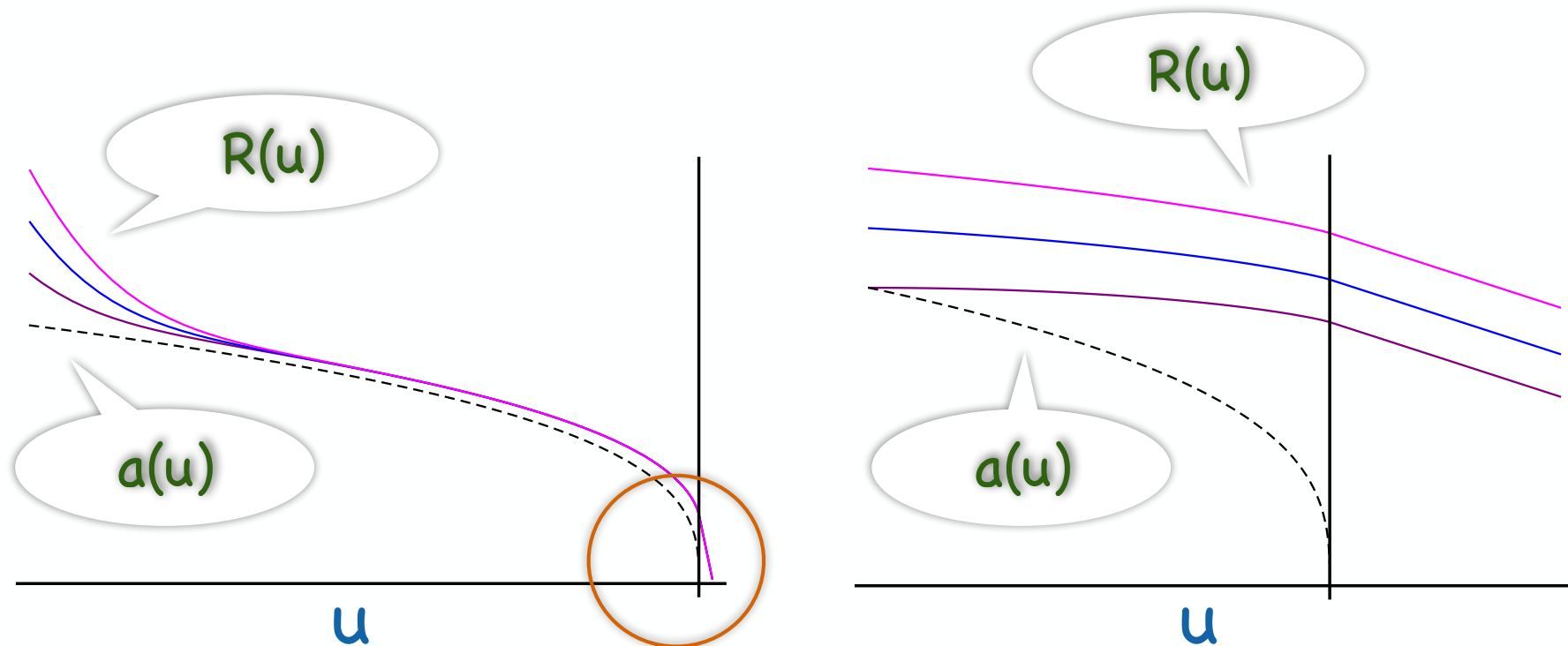
Light-like geodesics:

$$du = 0 \quad \left( 1 - \frac{a(u)}{r} \right) du + 2dr = 0$$

Outgoing

Ingoing for  $r > a$

## $R(u)$ vs $a(u)$



All infalling null trajectories are geodesically complete without crossing horizon. [KMY2013][Ho2015]



# Proof of no black-hole apparent horizon

[Ho2015]

Schwarzschild radius is space-like:

$$r = a(u)$$

$$ds^2 = 0du^2 - 2da(u)du = -2\dot{a}(u)du^2 > 0$$

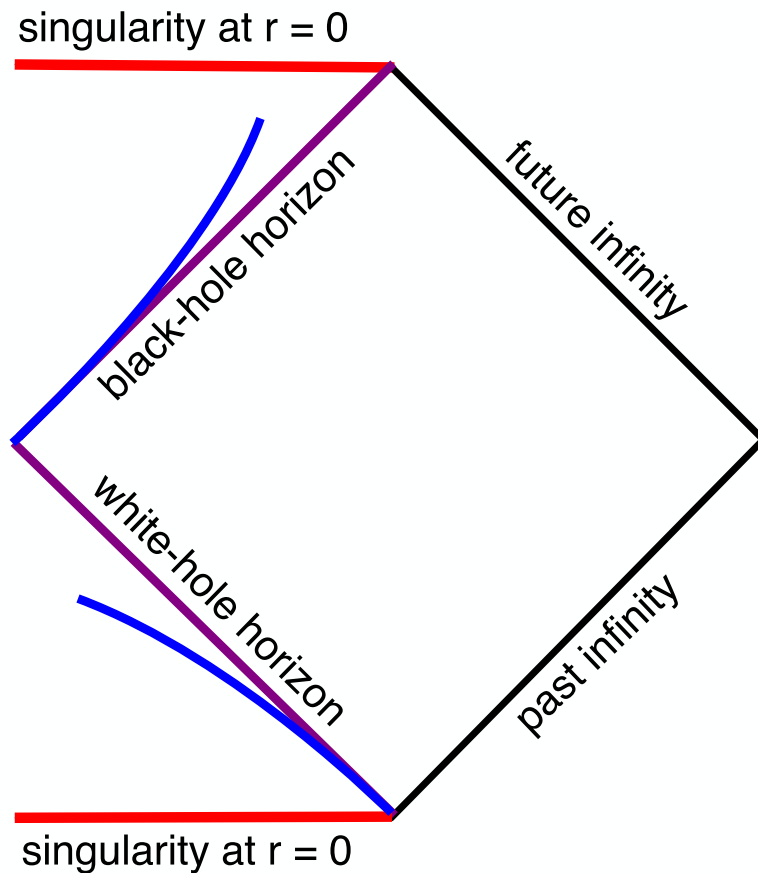
Schwarzschild radius shrinks faster than light!

Complete evaporation ( $a(u) = 0$  for  $u > u^*$ )

→ infalling trajectories are geodesically complete

⇒ No black-hole apparent horizon.

Outgoing radiation can be arbitrarily weak.



Black-hole apparent  
horizon vs white-hole  
apparent horizon

[KMY2013][Ho2015]

Schwarzschild solution is degenerate. [Ho2015]  
Gravitational collapse ~ critical phenomenon

# KMY Model

[Kawai-Matsuo-Yokokura 2013]

[Kawai-Yokokura 2014]

[Kawai-Yokokura 2015]

Assumptions:

Spherical Symmetry

Collapsing massless dust

(pre-)HR of massless particles

The energy-momentum tensor is that of a light-like energy flux outside the surface of the collapsing sphere.



# Outside the Collapsing Sphere

$r > R(u) > a(u)$ : the outgoing Vaidya metric [KMY2013]

$$ds^2 = - \left( 1 - \frac{a(u)}{r} \right) du^2 - 2du dr + r^2 d\Omega^2$$

$$a(u) = 2M(u) \quad T_{uu} = \frac{G_{uu}}{8\pi G} = -\frac{1}{8\pi G} \frac{\dot{a}(u)}{r^2}$$

Light-like geodesics:

$$du = 0 \quad \left( 1 - \frac{a(u)}{r} \right) du + 2dr = 0$$

Outgoing  
e.g. HR

Ingoing for  $r > a$   
e.g.  $r = R(u)$

# Information Loss Paradox

Apply the same arguments  $\Rightarrow$

If complete evaporation,

there is no horizon  $\Rightarrow$  No info loss

$\rightarrow$  **Asymptotic Black Hole**

a *consistent* approach.

No paradox even if there is horizon.

Collapsing matter is never behind a horizon.

(pre-)HR created near the collapsing matter,  
like peeling off an onion.

[KY2015]

- \* Burning through quantum tunnelling  
at macroscopic scale
- \* Hard to distinguish from a black hole.

# Misconception #2

The blue-shift factor approaches to infinity as the collapsing surface approaches to the Schwarzschild radius, and thus there would be a diverging energy flux near the collapsing surface, if Hawking radiation exists there.

## Surface of the collapsing sphere:

$$\frac{dR(u)}{du} = -\frac{1}{2} \left( 1 - \frac{a(u)}{R(u)} \right) \quad \dot{a}(u) \simeq -\frac{\sigma}{a^2(u)}$$

$$R(u) \simeq a(u) + \frac{2\sigma}{a(u)} \quad \sigma = \frac{NG\hbar}{48\pi}$$

The surface of a collapsing sphere stays above the Schwarzschild radius by the separation:

$$\Delta r = R - a \simeq \frac{2\sigma}{a}$$



# energy flux at collapsing surface

- The energy-momentum tensor near the outer surface of the shell is

$$T_{uu} = -\frac{1}{8\pi G} \frac{\dot{a}}{r^2} \qquad T_{ur} = T_{rr} = 0$$

$$\hat{n}^\mu = (\hat{n}^u, \hat{n}^r, 0, 0) \qquad \hat{n}^\mu \hat{n}_\mu = -1$$

$$\hat{n}^u = \frac{e^\zeta}{\sqrt{1 - a/r}} \qquad \hat{n}^r = -\sqrt{1 - a/r} \sinh \zeta$$

$$T_{\mu\nu} \hat{n}^\mu \hat{n}^\nu = -\frac{1}{8\pi G} \frac{\dot{a}}{r^2} \frac{e^{2\zeta}}{1 - a/r} \simeq \frac{1}{16\pi G} \frac{e^{2\zeta}}{a^2}$$

which is very weak for a large aBH.

[Ho2015]



Hawking radiation in the absence of  
black-hole apparent horizon?

→ pre-Hawking radiation

# Hawking radiation without horizon?

## Bogoliubov transformation:

Exponential relation between  $u$  and  $U$ .

[Barcelo-Liberati-Sonego-Visser 1011.5911]

$R > a \Rightarrow$  no horizon

$R - a = \Delta r = \textit{extremely small}$

Hawking radiation of wavelengths  $\lambda \gg \Delta r$   
are expected to appear.

# Hawking radiation for white-hole horizon?

same spectrum of Hawking radiation [KMY2013]

# Generalization

incomplete evaporation

generalized solution w. spherical symmetry

general Hawking radiation

more general energy-momentum tensor

[Ho2015]

The arguments are robust.

# geometry inside the collapsing sphere

Decompose the collapsing sphere into infinitely many infinitesimally thin shells.

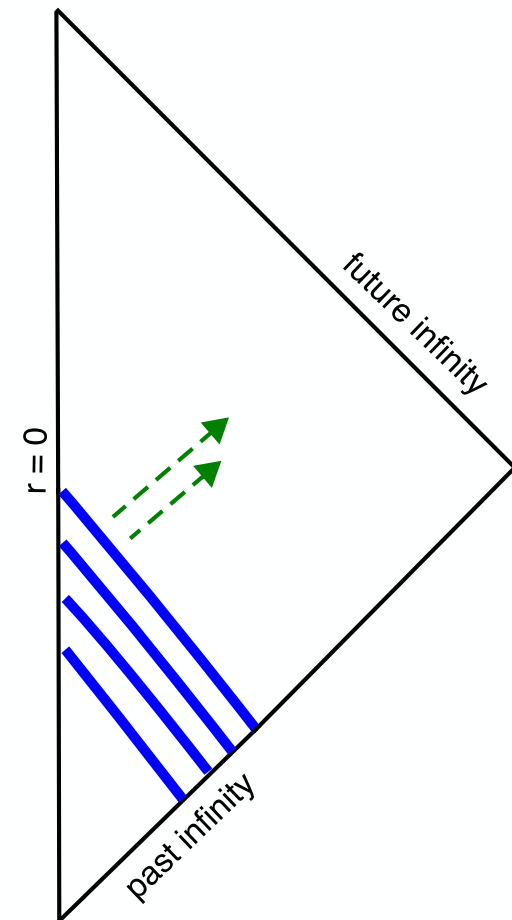
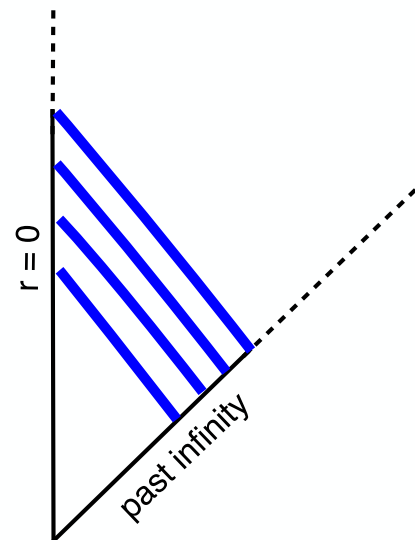
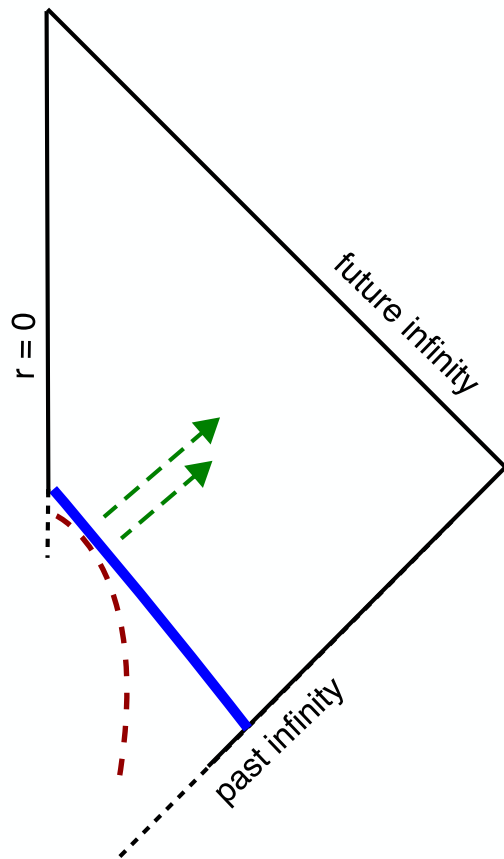
Every layer approaches to the Schwarzschild radius.

Huge red-shift => everything inside is frozen.

[KMY2013,KY2014,KY2015]

# KMY Model: Patching Penrose diagrams together

[KMY2013]



# Asymptotic Black Holes

Surface stays at  $\Delta r \sim 2\sigma/a$

away from the Schwarzschild radius  $a$ .

~ Brick Wall Model and Membrane Paradigm.

[Ho2016]

\* Thin-shell model is not reliable.



# Black Hole (Non-) Formation

Trapping region: Frolov, Vilkoviski (81)

Domain wall: Vachaspati-Stojkovic-Krauss [0609024]

Collapsing star: Mersini-Houghton [1406.1525]

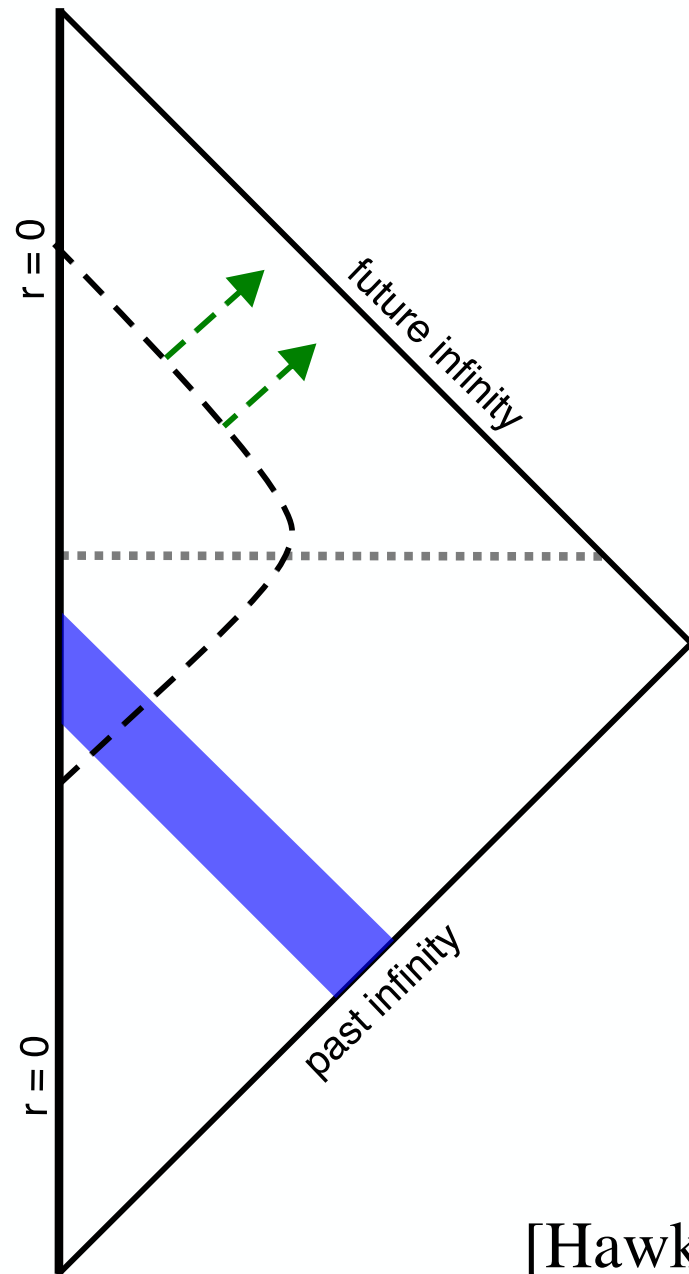
Fuzzball: Lunin-Mathur [0109154, 0202072]

Firewall: Almheiri-Marolf-Polchinski-Sully [1207.3123];  
Braunstein [0907.1190]

Review: Mathur [09091038]

“No drama at horizon” vs “Order 1 correction”

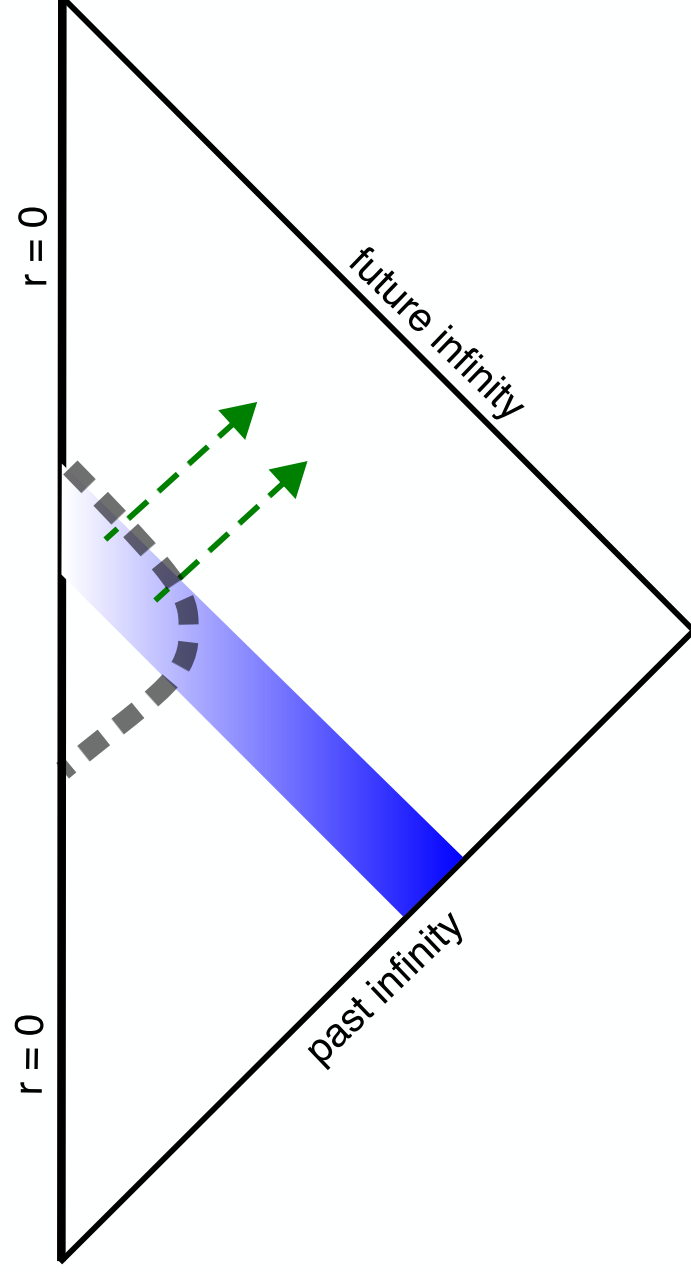
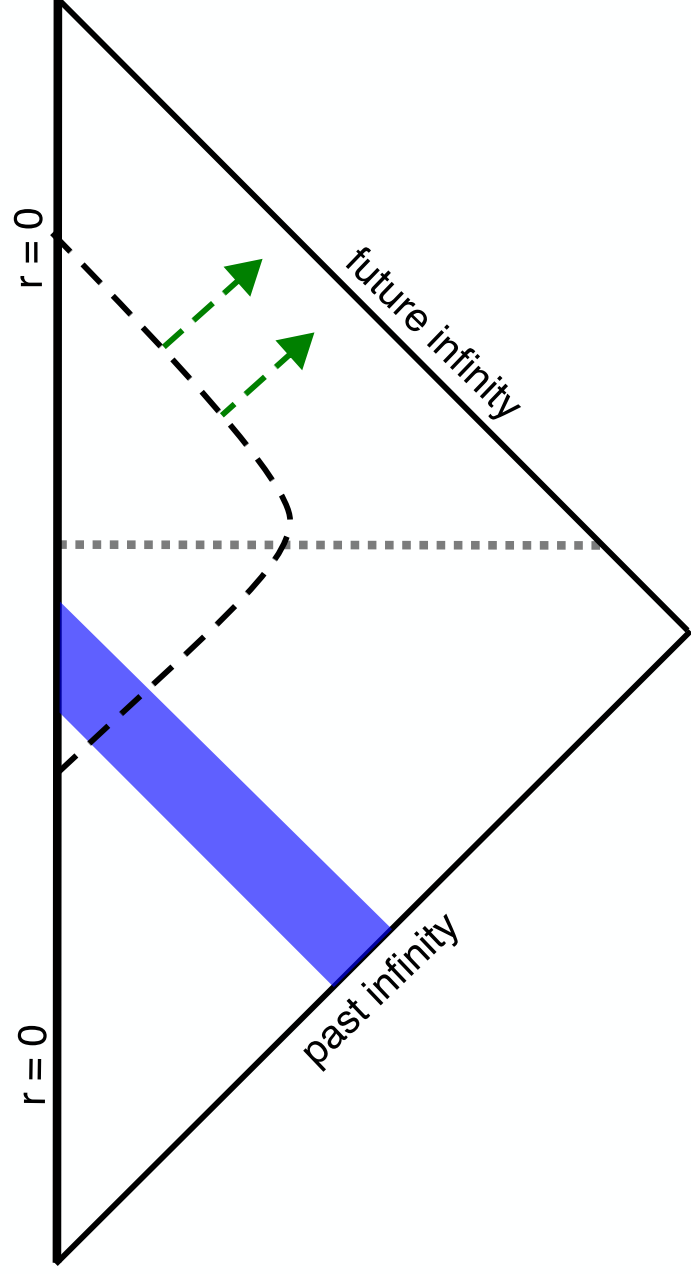
What's new: robust semi-classical arguments.



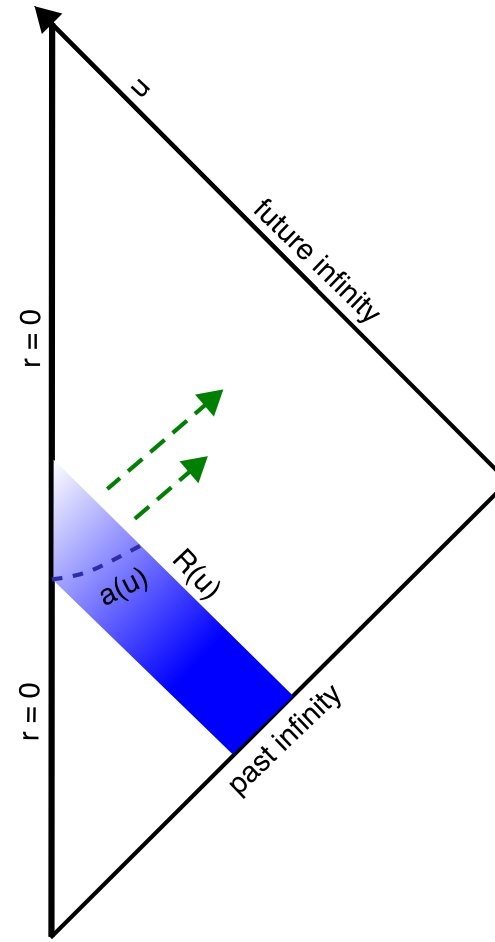
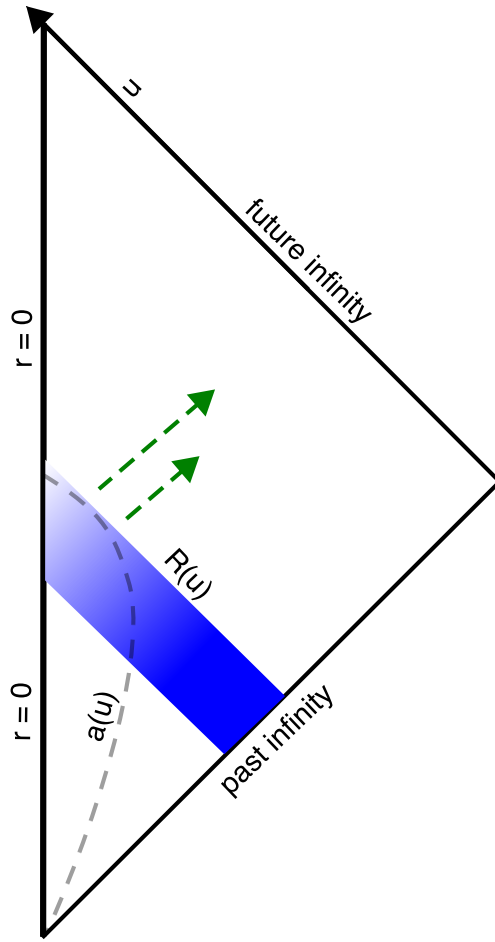
If there is classical radiation coming out of the horizon, it is a *white-hole* horizon.

Firewall persists?

[Hawking-Perry-Strominger 2016]



# KMY Model

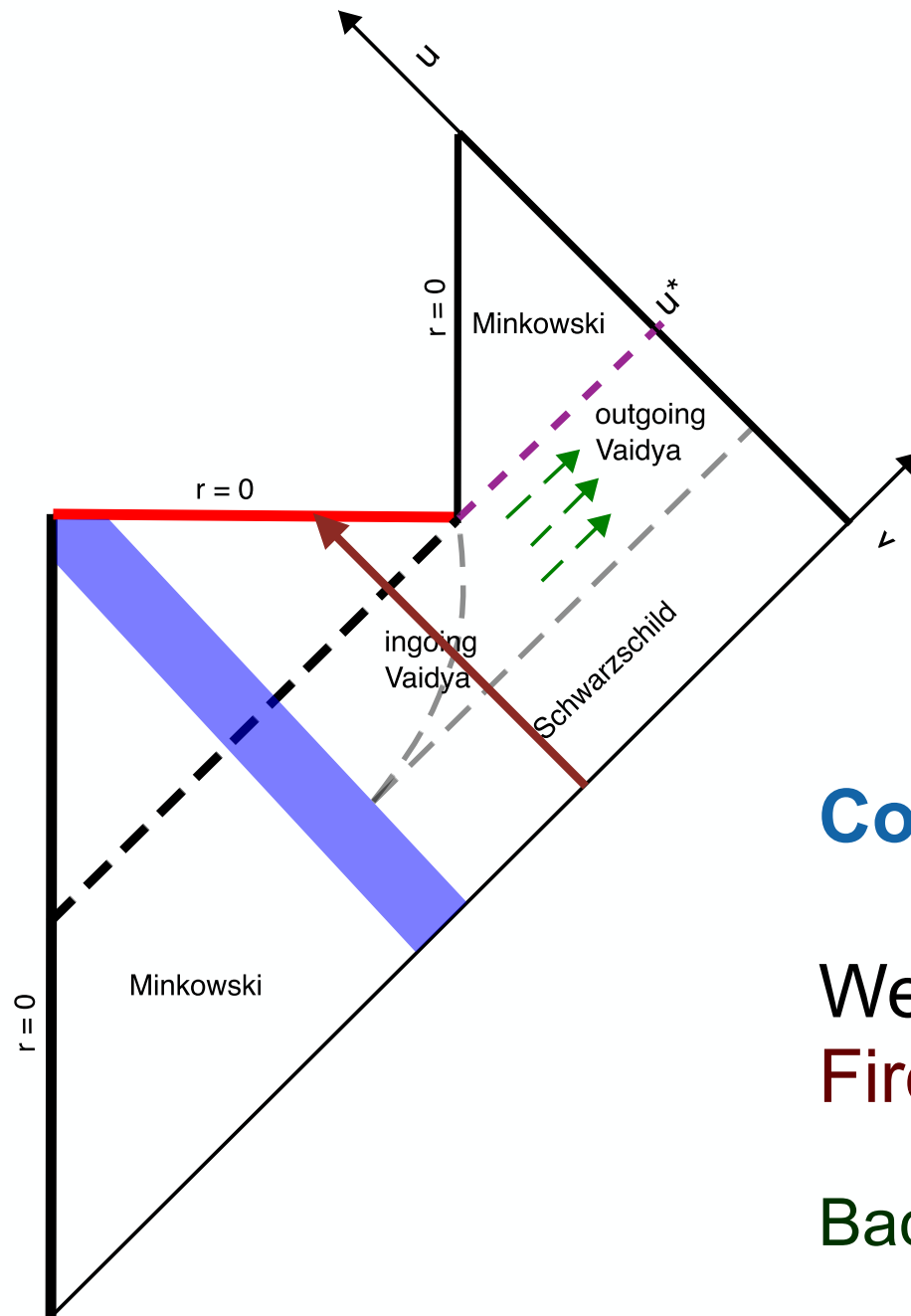


# Conclusion

- Consistent model of black holes
- Semi-classical, large scale physics
- No firewall
- No horizon (if not already there)
- No Information loss paradox
- Asymptotic black holes in observations

Thank you!



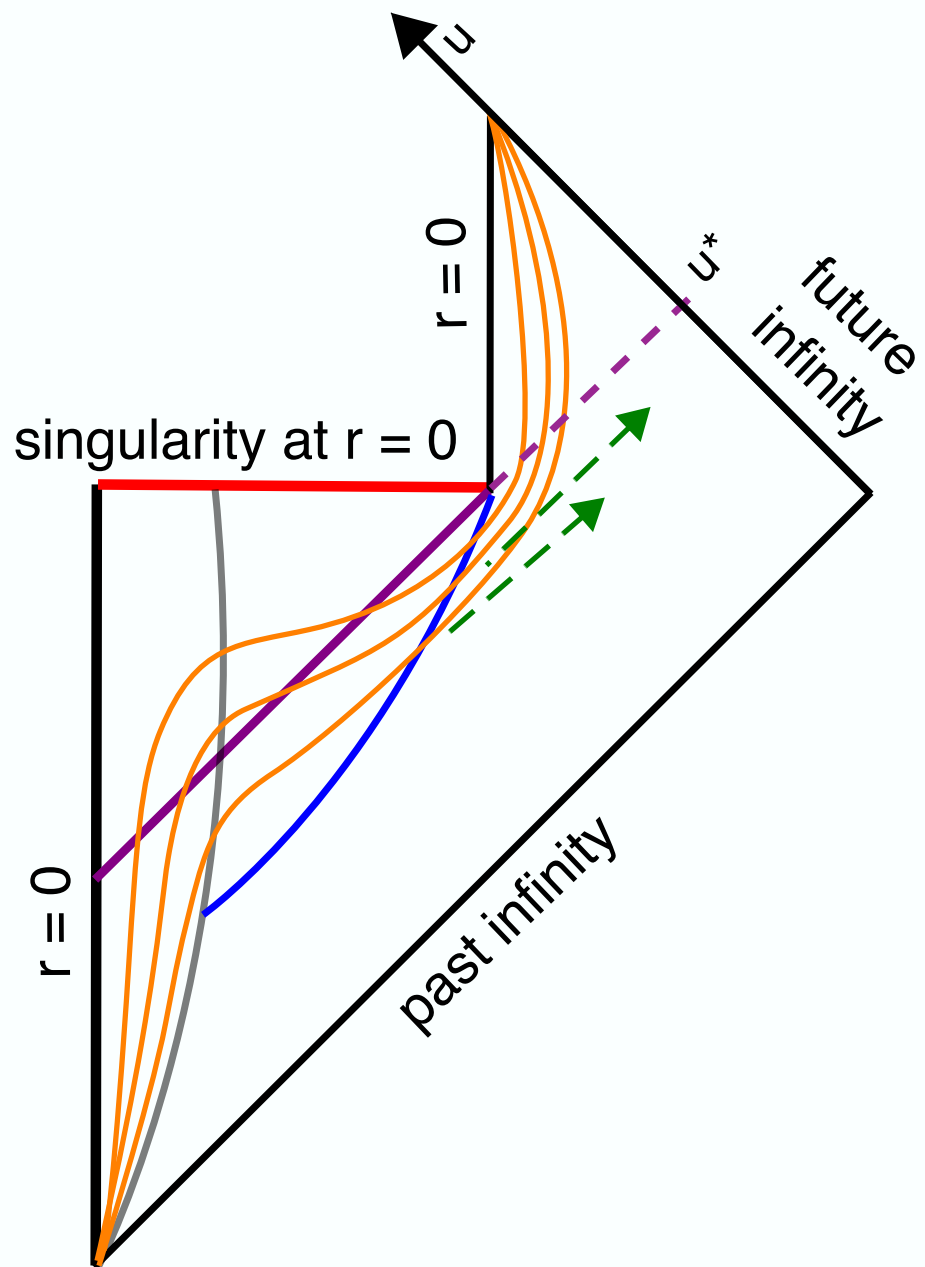


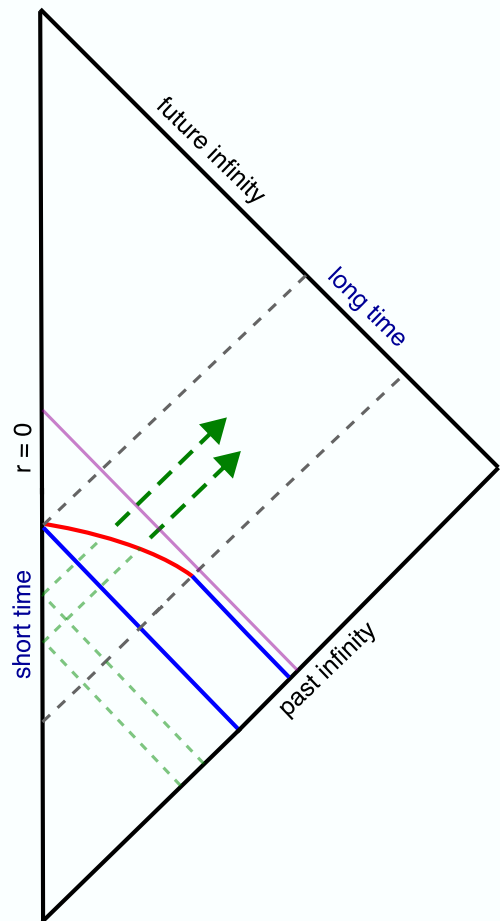
## Conventional Model:

Weak energy condition violated.  
**Firewall** at the horizon.

[AMPS: 1207.3123]

Back-reaction?





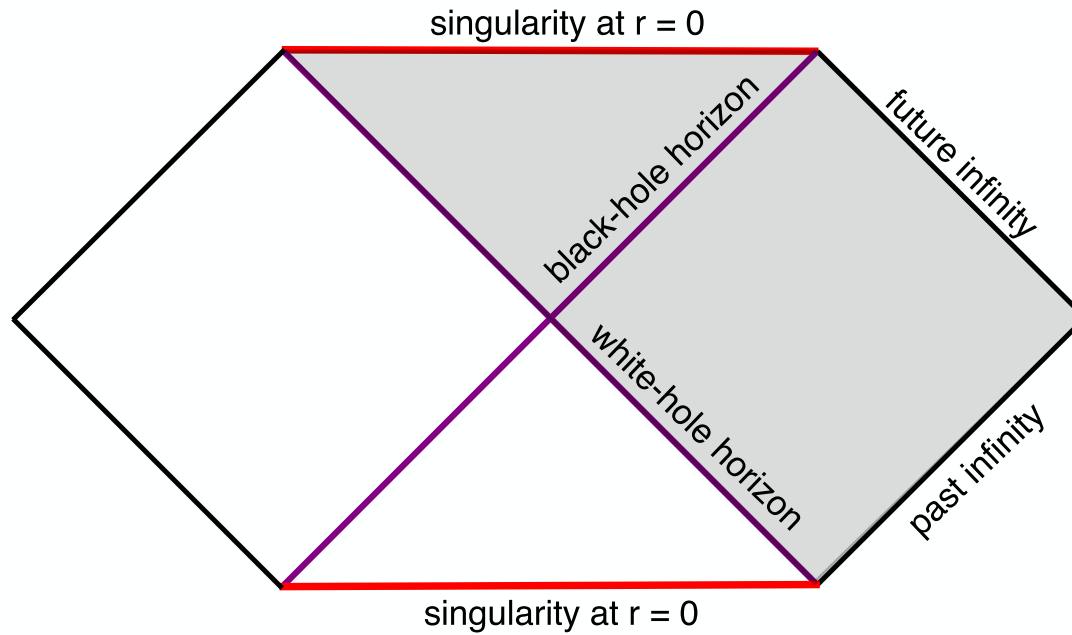
## **Thin Shell and Time Scale**

The thin shell model is not a good approximation because over a long period of time the inner surface and the outer surface must be separated by the Schwarzschild radius.

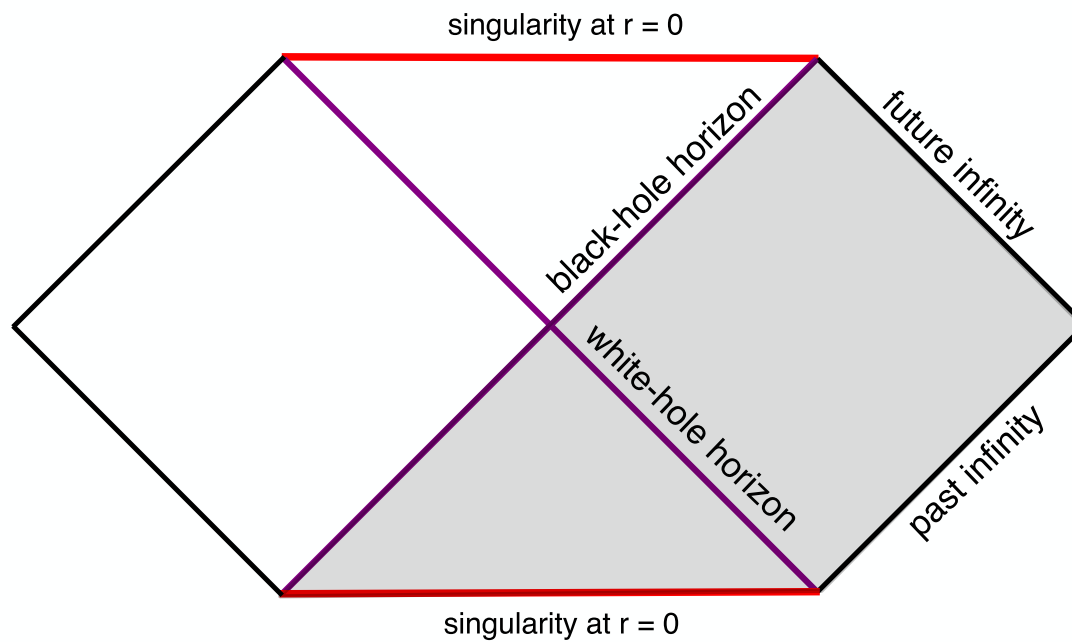
## Perturbative Approximation?

Schwarzschild solution is degenerate. [Ho2015]

Gravitational collapse ~ critical phenomenon



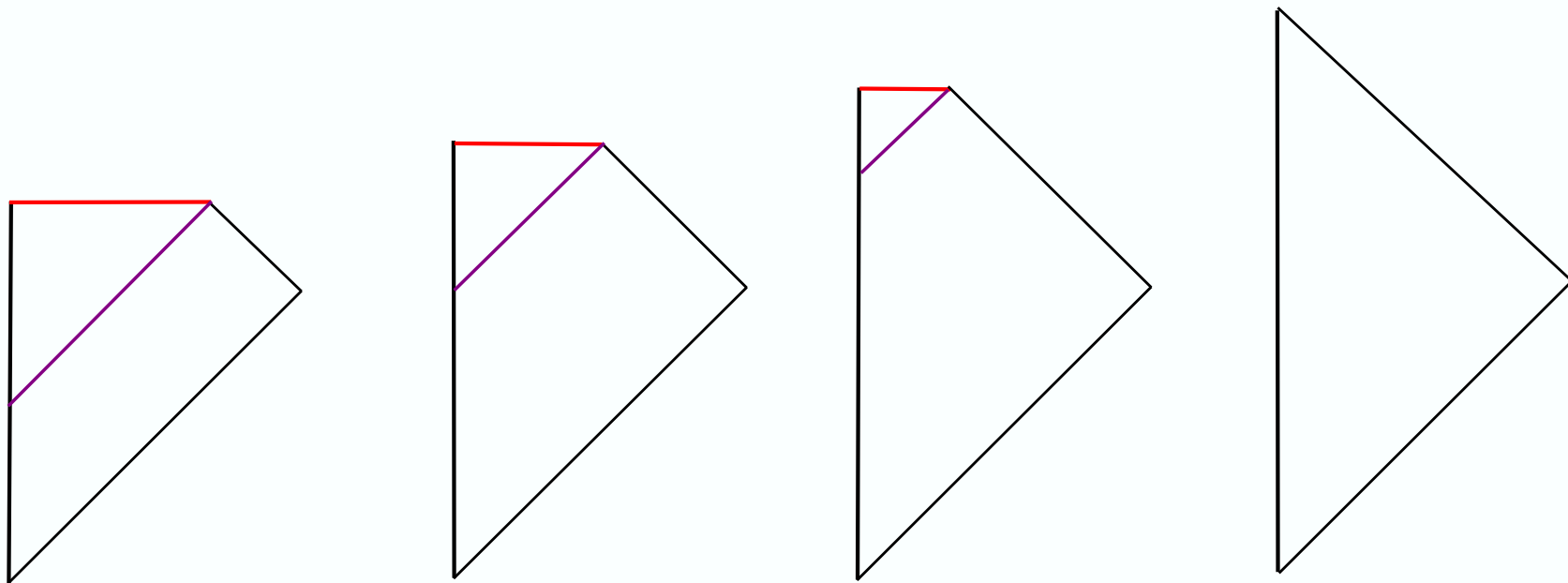
black-hole



white-hole



- **Continuous Deformation of Classical Black Hole by Hawking Radiation**
- From a classical black hole without HR to larger and larger HR,
- to complete evaporation.



The coordinate system of  $(u, r)$  only covers the part visible to a distant observer (outside the horizon).

## Infalling observer's crossing in (in)finite time:

$$ds^2 = - \left( 1 - \frac{a(u)}{r} \right) du^2 - 2dudr + r^2 d\Omega^2$$

Recall that if  $a = \text{constant}$ ,

$$u = t - r^* \qquad r^* = r + a_0 \log \left| \frac{r}{a_0} - 1 \right|$$

For an infalling observer, the relevant time coordinate is

$$v = t + r^*$$

It can be finite when  $t$  is infinite if  $r = a$ .

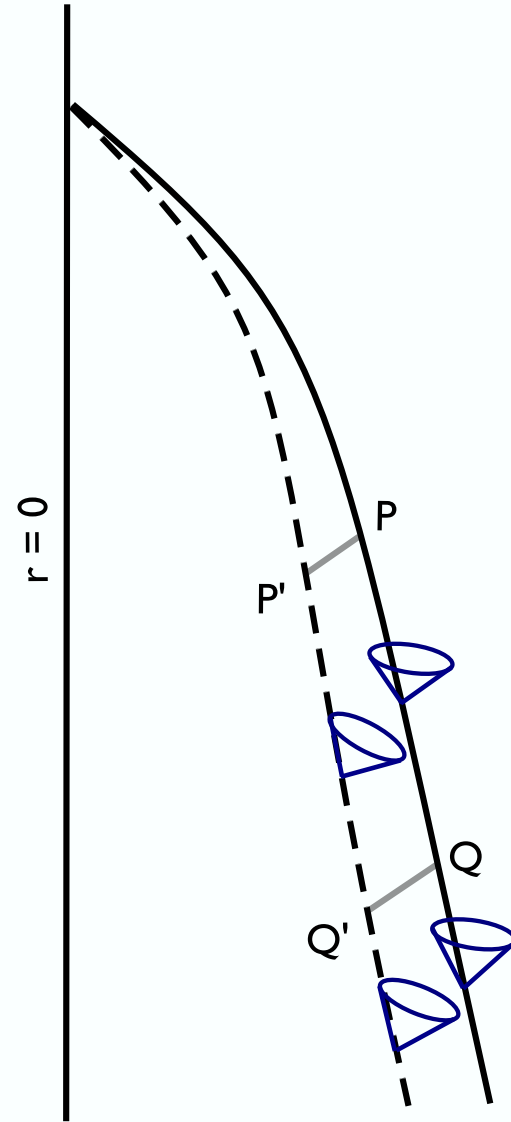
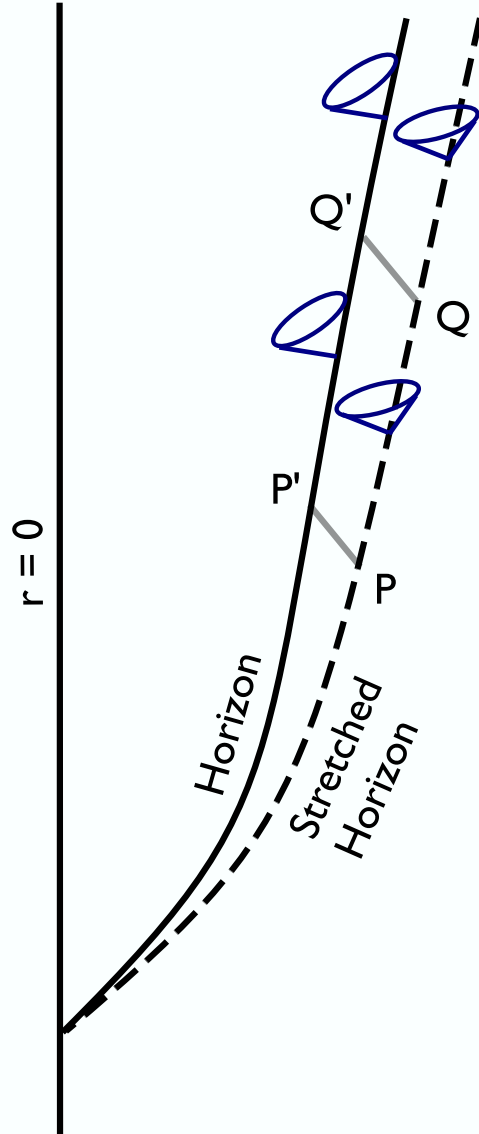
But it works only if there is no complete evaporation.

[Ho2015]

## Semi-classical approximation

- Appearance of Planck scale may not have to do with Planckian physics. (e.g. constant acceleration towards light cone)
- Planck scale in 4D is not necessarily the string scale.
- Number of species  $N$  can be large.
- Large energy-momentum tensor only for  $r < R$ .

# Membrane Paradigm



[Ho2015]

$$\hat{n}^\mu = (\hat{n}^u, \hat{n}^r, 0, 0)$$

$$\hat{\ell}^\mu = (\hat{\ell}^u, \hat{\ell}^r, 0, 0)$$

$$\hat{n}^u = \frac{e^\zeta}{\sqrt{1 - a/r}}$$

$$\hat{n}^r = -\sqrt{1 - a/r} \sinh \zeta$$

$$\hat{\ell}^u = \mp \frac{e^\zeta}{\sqrt{1 - a/r}}$$

$$\hat{\ell}^r = \pm \sqrt{1 - a/r} \cosh \zeta$$

$$\hat{n}^\mu \hat{n}_\mu = -1 \quad \hat{\ell}^\mu \hat{\ell}_\mu = 1 \quad \hat{n}^\mu \hat{\ell}_\mu = 0$$

$$T_{\mu\nu} \hat{n}^\mu \hat{n}^\nu = T_{\mu\nu} \hat{\ell}^\mu \hat{\ell}^\nu = \mp T_{\mu\nu} \hat{n}^\mu \hat{\ell}^\nu$$

$$T_{\mu\nu} \hat{n}^\mu \hat{n}^\nu = -\frac{1}{8\pi G} \frac{\dot{a}}{r^2} \frac{e^{2\zeta}}{1 - a/r} \simeq \frac{1}{16\pi G} \frac{e^{2\zeta}}{a^2}$$

# Hawking Radiation

[KMY2013]

$$\dot{a}(u) = -\frac{NG\hbar}{4\pi}\{u, U\} \qquad \{u, U\} \equiv \frac{\ddot{U}^2}{\dot{U}^2} - \frac{2\ddot{U}}{3\dot{U}}$$

$$\dot{a}(u) \simeq -\frac{\sigma}{a^2(u)} \qquad \sigma = \frac{NG\hbar}{48\pi}$$

$$a(u) \simeq \begin{cases} (3\sigma)^{1/3}(u^* - u)^{1/3} & u < u^* \\ 0 & u \geq u^* \end{cases}$$